

# Lecture 06

# Arithmetic Instructions

CS213 – Intro to Computer Systems  
Branden Gena – Winter 2024

Slides adapted from:

St-Amour, Hardavellas, Bustamente (Northwestern), Bryant, O'Hallaron (CMU), Garcia, Weaver (UC Berkeley)

# Administrivia

- Pack Lab due Thursday by midnight
  - Expect office hours to start getting very busy
  - Morning office hours today were totally empty though...
- Bomb Lab releases today or tomorrow
  - Practice interpreting assembly code
  - Due after the midterm exam
    - But we strongly recommend you start it early as assembly practice
  - Partnership survey will go out on Piazza soon

# Administrivia

- Midterm exam in 1.5 weeks
  - Class time next week Thursday (February 1<sup>st</sup>)
  - Covers everything from the start of class through Control Flow
    - Does NOT cover function calls in assembly (“Procedures” lecture next week)
  - Bring a pencil and one 8.5”x11” inch paper with notes
    - Notes can be on both sides, handwritten or typed
  - No calculators
  - Practice exams (and solutions) are on the Canvas home page
  - Also good practice: Homework 2 (due Tuesday), phases 1-3 of Bomb Lab
- ANU students: I’ll reach out this week with details

# Instruction Set Architecture sits at software/hardware interface

Source code

Different applications  
or algorithms

Compiler

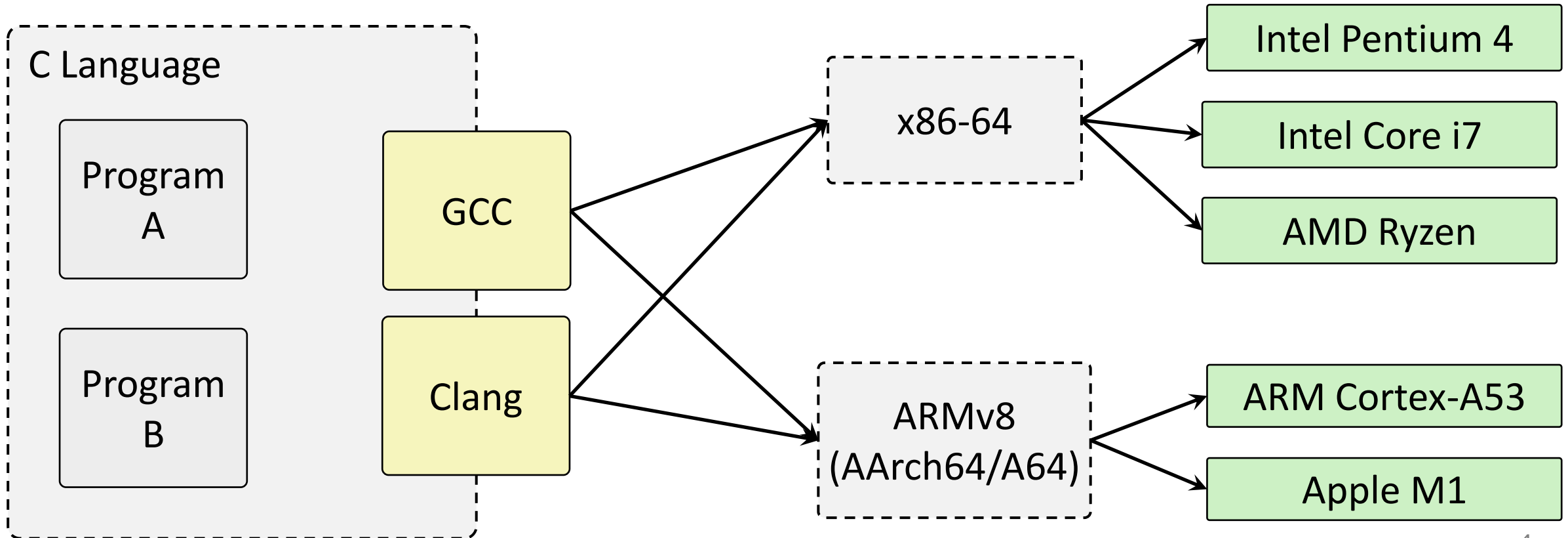
Perform optimizations,  
generate instructions

Architecture

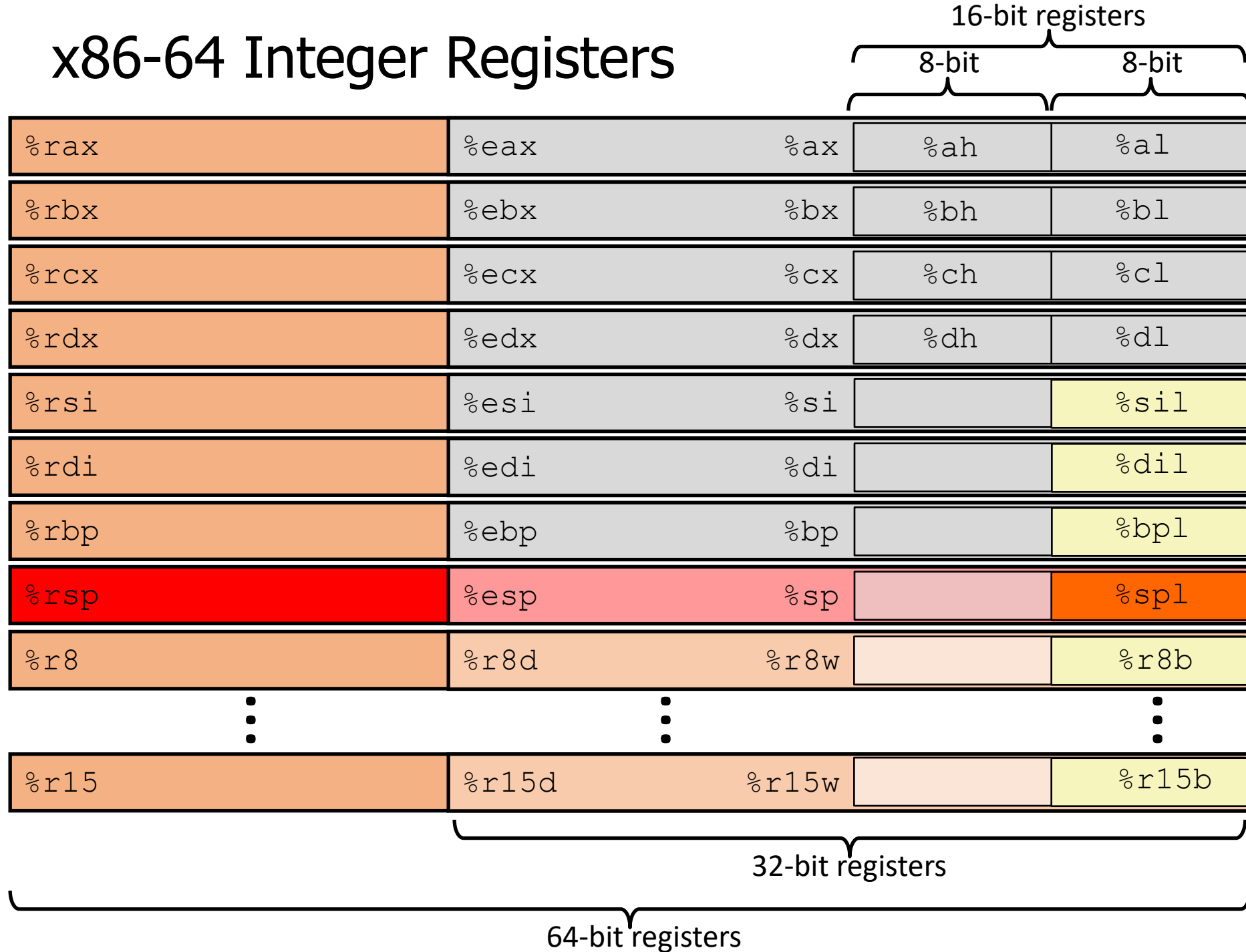
Instruction set

Hardware

Different  
implementations



# x86-64 Integer Registers



# Three Basic Kinds of Instructions

## 1. Transfer data between memory and register

- *Load* data from memory into register
  - `%reg = Mem[address]`
- *Store* register data into memory
  - `Mem[address] = %reg`

*Remember:* Memory is indexed just like an array of bytes!

## 2. Perform arithmetic operation on register or memory data

- `c = a + b;`      `z = x << y;`      `i = h & g;`

## 3. Control flow: what instruction to execute next

- Unconditional jumps to/from procedures
- Conditional branches

**In x86-64 these basic types can often be combined**

# Operand Combinations

|      | Source | Dest | Src, Dest           | C Analog       |
|------|--------|------|---------------------|----------------|
| movq | Imm    | Reg  | movq \$0x4, %rax    | var_a = 0x4;   |
|      |        | Mem  | movq \$-147, (%rax) | *p_a = -147;   |
|      | Reg    | Reg  | movq %rax, %rdx     | var_d = var_a; |
|      |        | Mem  | movq %rax, (%rdx)   | *p_d = var_a;  |
|      | Mem    | Reg  | movq (%rax), %rdx   | var_d = *p_a;  |

Cannot do memory-memory transfer with a single instruction

# Today's Goals

- Continue exploring x86-64 assembly
  - Arithmetic
- Discuss real-world x86-64
  - Special cases
  - Generating assembly
- Understand condition codes
  - Method for testing Boolean conditions



# Outline

- **Arithmetic Instructions**
- Special Cases
  - Non 64-bit Data
  - Load Effective Address
- Condition Codes
- Viewing x86-64 Assembly

# Some arithmetic operations

## • Two-operand instructions

| Instruction             | Effect                    | Description  |
|-------------------------|---------------------------|--------------|
| <code>addq S, D</code>  | $D \leftarrow D + S$      | Add          |
| <code>subq S, D</code>  | $D \leftarrow D - S$      | Subtract     |
| <code>imulq S, D</code> | $D \leftarrow D * S$      | Multiply     |
| <code>xorq S, D</code>  | $D \leftarrow D \wedge S$ | Exclusive or |
| <code>orq S, D</code>   | $D \leftarrow D   S$      | Or           |
| <code>andq S, D</code>  | $D \leftarrow D \& S$     | And          |

## • Shifts

| Instruction            | Effect                 | Description                             |
|------------------------|------------------------|---|
| <code>sarq k, D</code> | $D \leftarrow D \gg k$ | Shift arithmetic right                  |
| <code>shrq k, D</code> | $D \leftarrow D \gg k$ | Shift logical right                     |
| <code>salq k, D</code> | $D \leftarrow D \ll k$ | Shift left                              |
| <code>shlq k, D</code> | $D \leftarrow D \ll k$ | Shift left (same as <code>salq</code> ) |

## Operand types

- Immediate
  - Register
  - Memory
- (Only one can be memory)

Be careful with operand order!!!  
(Matters for some operations)

# A note on instruction names

- Instruction names can look somewhat arcane
  - `shlq?` `movzb1?`



**PowerPC Instructions**

@ppcinstructions

Follow



`rlwbv` - Rotate Left Wheel and Buy a Vowel

- But, good news: names (usually) follow conventions
  - Common prefixes (`add`), suffixes (`b`, `w`, `l`, `q`), etc.
  - So you can understand pieces separately
  - Then combine their meanings

# Some Arithmetic Operations

- Unary (one-operand) Instructions:

| Instruction         | Effect                | Description |
|---------------------|-----------------------|-------------|
| <code>incq D</code> | $D \leftarrow D + 1$  | Increment   |
| <code>decq D</code> | $D \leftarrow D - 1$  | Decrement   |
| <code>negq D</code> | $D \leftarrow -D$     | Negate      |
| <code>notq D</code> | $D \leftarrow \sim D$ | Complement  |

- See textbook Section 3.5.5 for more instructions:  
`mulq`, `cqto`, `idivq`, `divq`

# Converting C to Assembly

op src, dst

- Suppose  $a \rightarrow \%rax$ ,  $b \rightarrow \%rbx$ ,  $c \rightarrow \%rcx$   
Convert the following C statement to x86-64:

`a = b + c;`

# Converting C to Assembly

op src, dst

- Suppose  $a \rightarrow \%rax$ ,  $b \rightarrow \%rbx$ ,  $c \rightarrow \%rcx$   
Convert the following C statement to x86-64:

`a = b + c;`

```
movq %rbx, %rax      (a = b;)  
addq %rcx, %rax      (a += c;)
```

# Converting C to Assembly

op src, dst

- Suppose  $a \rightarrow \%rax$ ,  $b \rightarrow \%rbx$ ,  $c \rightarrow \%rcx$   
Convert the following C statement to x86-64:

```
a = b + c;
```

```
movq    $0, %rax  
addq   %rbx, %rax  
addq   %rcx, %rax
```

Is this okay?

# Converting C to Assembly

op src, dst

- Suppose  $a \rightarrow \%rax$ ,  $b \rightarrow \%rbx$ ,  $c \rightarrow \%rcx$   
Convert the following C statement to x86-64:

```
a = b + c;
```

```
movq    $0, %rax  
addq   %rbx, %rax  
addq   %rcx, %rax
```

Is this okay?

Yes: just a little slower



# Converting C to Assembly

op src, dst

- Suppose  $a \rightarrow \%rax$ ,  $b \rightarrow \%rbx$ ,  $c \rightarrow \%rcx$   
Convert the following C statement to x86-64:

```
a = b + c;
```

```
addq %rbx, %rcx  
movq %rcx, %rax
```

Is this okay?

# Converting C to Assembly

op src, dst

- Suppose  $a \rightarrow \%rax$ ,  $b \rightarrow \%rbx$ ,  $c \rightarrow \%rcx$   
Convert the following C statement to x86-64:

```
a = b + c;
```

```
addq %rbx, %rcx  
movq %rcx, %rax
```

Is this okay?

No: it overwrites C  
which could still be  
used later in code!

## Question + Break

### *Reminder*

`addq, src, dst → dst = dst + src`

- Suppose `a → %rax`, `b → %rbx`, `c → %rcx`  
Convert the following C statement to x86-64:

`c = (a-b) + 5;`

[A]

```
movq %rax, %rcx
subq %rbx, %rcx
addq $5, %rcx
```

[C]

```
subq %rcx, %rax, %rbx
addq %rcx, %rcx, $5
```

[B]

```
movq %rax, %rcx
subq %rbx, %rcx
movq $5, %rcx
```

[D]

```
subq %rbx, %rax
addq $5, %rax
movq %rax, %rcx
```

# Question + Break

*Reminder:* `addq, src, dst`  $\rightarrow$  `dst = dst + src`

- Suppose `a`  $\rightarrow$  `%rax`, `b`  $\rightarrow$  `%rbx`, `c`  $\rightarrow$  `%rcx`  
Convert the following C statement to x86-64:

`c = (a-b) + 5;`

[A]

```
movq %rax, %rcx
subq %rbx, %rcx
addq $5, %rcx
```

[B]

```
movq %rax, %rcx
subq %rbx, %rcx
movq $5, %rcx
```

`c = 5`

[C]

```
subq %rcx, %rax, %rbx
addq %rcx, %rcx, $5
```

Not x86

[D]

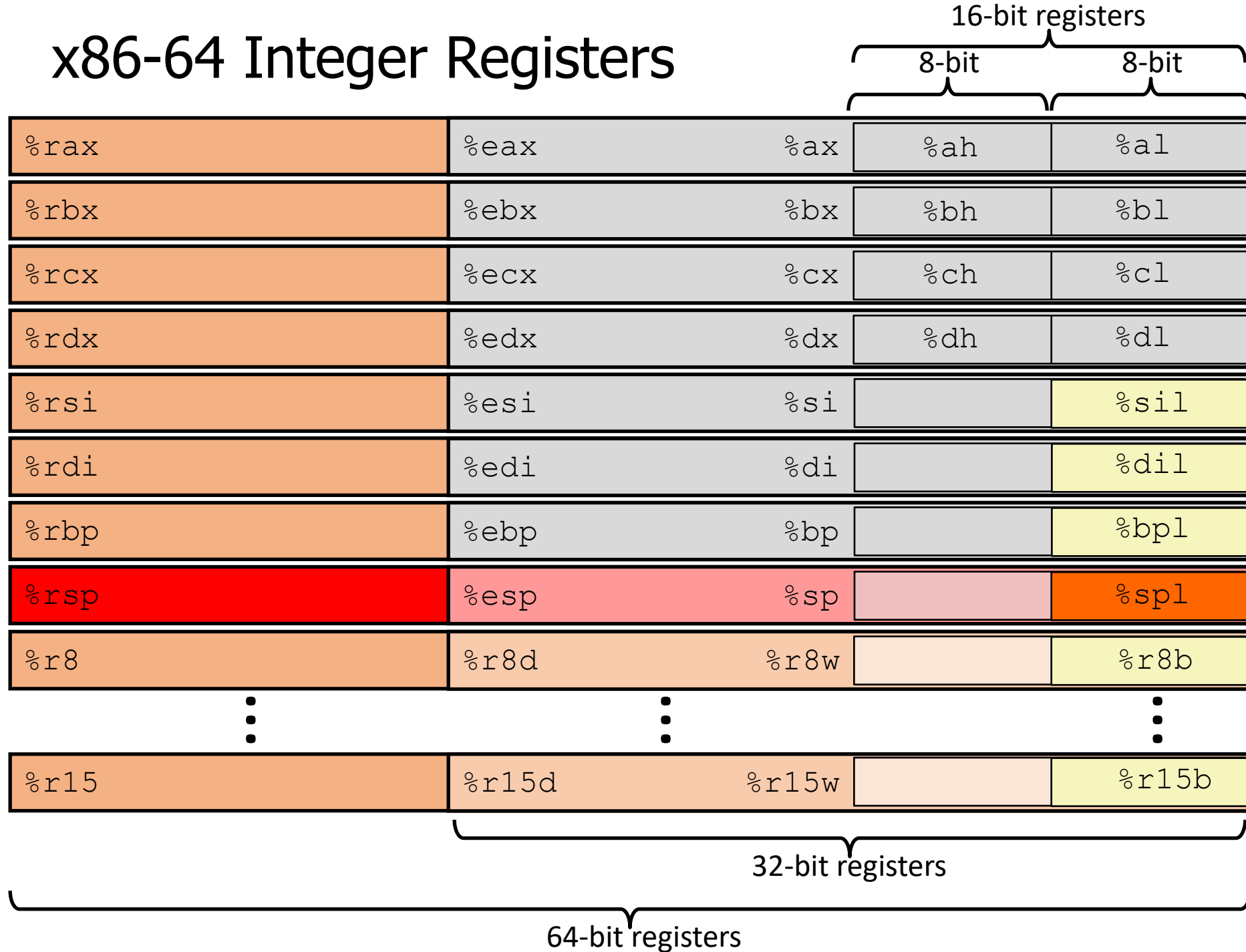
```
subq %rbx, %rax
addq $5, %rax
movq %rax, %rcx
```

Overwrites  
a

# Outline

- Arithmetic Instructions
- **Special Cases**
  - **Non 64-bit Data**
  - Load Effective Address
- Condition Codes
- Viewing x86-64 Assembly

# x86-64 Integer Registers



# Moving data of different sizes

- “Vanilla” move can only move between source and dest of the same size
  - Larger → smaller: use the smaller version of registers
  - Smaller → larger: extension! We have two options: zero-extend or sign-extend

| Instruction  | Effect   | Description   |
|--|--|---|
| <code>movX S,D</code><br>$X \in \{q, l, w, b\}$                | $D \leftarrow S$   | Copy quad-word (8B), long-word (4B), word (2B) or byte (1B) |
| <code>movsXX S,D</code><br>$XX \in \{bw, bl, wl, bq, wq, lq\}$ | $D \leftarrow \text{SignExtend}(S)$                          | Copy sign-extended byte to word, byte to long-word, etc.    |
| <code>movzXX S,D</code><br>$XX \in \{bw, bl, wl, bq, wq, lq\}$ | $D \leftarrow \text{ZeroExtend}(S)$                          | Copy zero-extended byte to word, byte to long-word, etc.    |
| <code>cltq</code><br>(convert long to quad)                    | <code>%rax</code> $\leftarrow$ <code>SignExtend(%eax)</code> | Sign-extend <code>%eax</code> to <code>%rax</code>          |

# Example: moving byte data

op src, dst

- Note the differences between `movb`, `movsbl` and `movzbl`
- Assume `%dl = 0xCD`, `%eax = 0x98765432`

`movb %dl, %al`                      `%eax = 0x987654CD`

`movsbl %dl, %eax`                    `%eax = 0xFFFFFFFFCD`

`movzbl %dl, %eax`                    `%eax = 0x000000CD`



# 32-bit Instruction Peculiarities

op src, dst

- Instructions that move or generate 32-bit values also set the upper 32 bits of the respective 64-bit register to zero, while 16 or 8 bit instructions don't.

```
movabsq $0xffffffffffffffff, %rax # rax = 0xffffffffffffffff
movb $0, %al # rax = 0xfffffffffff00
movw $0, %ax # rax = 0xfffffffffff0000
movl $0, %eax # rax = 0x0000000000000000
```

- This includes 32-bit arithmetic! (e.g., addl)

# Outline

- Arithmetic Instructions
- **Special Cases**
  - Non 64-bit Data
  - **Load Effective Address**
- Condition Codes
- Viewing x86-64 Assembly

# Complete Memory Addressing Modes

- **General:**

- $D (Rb, Ri, S)$

- $Rb$ : Base register (any register)

- $Ri$ : Index register (any register except `%rsp`)

- $S$ : Scale factor (1, 2, 4, 8) (sizes of common C types)

- $D$ : Constant displacement value (a.k.a. immediate)

- $\text{Mem}[ \text{Reg}[Rb] + \text{Reg}[Ri] * S + D ]$

# Saving computed addresses

- Generally, any instruction with ( ) in it, accesses memory
  - Address is computed first
  - Loads from memory if in a source operand
  - Stores into memory if in a destination operand
- But what if what you really want is the address?
  - `lea` – load effective address
  - Exception to ( ) rule. Does NOT access memory
  - Also used for arbitrary arithmetic
    - This is the compiler's *favorite* instruction

# Address computation instruction

- **leaq src, dst**
  - "leaq" stands for *load effective address*
  - **src** MUST be an address expression (any of the formats we've seen)
  - **dst** is a register
  - Sets **dst** to the *address* computed by the **src** expression  
(**does not go to memory! – it just does math**)
  - Example: `leaq (%rdx,%rcx,4), %rax`
- **Uses:**
  - Computing addresses without a memory reference
    - *e.g.* translation of `p = &x[i];`
  - Computing arithmetic expressions of the form  $x+k*i+d$ 
    - Though  $k$  can only be 1, 2, 4, or 8

# Example: `lea` VS. `mov`

| Registers         |       | Memory | Word Address |
|-------------------|-------|--------|--------------|
| <code>%rax</code> |       | 0x400  | 0x120        |
| <code>%rbx</code> |       | 0xF    | 0x118        |
| <code>%rcx</code> | 0x2   | 0x8    | 0x110        |
| <code>%rdx</code> | 0x100 | 0x10   | 0x108        |
| <code>%rdi</code> |       | 0x1    | 0x100        |
| <code>%rsi</code> |       |        |              |

```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```

# Example: `lea` VS. `mov`

## Registers

|                   |                           |
|-------------------|---------------------------|
| <code>%rax</code> | <b><code>0x108</code></b> |
| <code>%rbx</code> |                           |
| <code>%rcx</code> | <code>0x2</code>          |
| <code>%rdx</code> | <code>0x100</code>        |
| <code>%rdi</code> |                           |
| <code>%rsi</code> |                           |

## Memory

|                    | Word Address       |
|--------------------|--------------------|
| <code>0x400</code> | <code>0x120</code> |
| <code>0xF</code>   | <code>0x118</code> |
| <code>0x8</code>   | <code>0x110</code> |
| <code>0x10</code>  | <code>0x108</code> |
| <code>0x1</code>   | <code>0x100</code> |

```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```

# Example: `lea` VS. `mov`

## Registers

|                   |                           |
|-------------------|---------------------------|
| <code>%rax</code> | <b><code>0x108</code></b> |
| <code>%rbx</code> | <b><code>0x10</code></b>  |
| <code>%rcx</code> | <code>0x2</code>          |
| <code>%rdx</code> | <code>0x100</code>        |
| <code>%rdi</code> |                           |
| <code>%rsi</code> |                           |

## Memory

|                    | Word Address       |
|--------------------|--------------------|
| <code>0x400</code> | <code>0x120</code> |
| <code>0xF</code>   | <code>0x118</code> |
| <code>0x8</code>   | <code>0x110</code> |
| <code>0x10</code>  | <code>0x108</code> |
| <code>0x1</code>   | <code>0x100</code> |

```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```



# Example: `lea` VS. `mov`

## Registers

|                   |                           |
|-------------------|---------------------------|
| <code>%rax</code> | <b><code>0x108</code></b> |
| <code>%rbx</code> | <b><code>0x10</code></b>  |
| <code>%rcx</code> | <code>0x2</code>          |
| <code>%rdx</code> | <code>0x100</code>        |
| <code>%rdi</code> | <b><code>0x100</code></b> |
| <code>%rsi</code> |                           |

## Memory

|                    | Word Address       |
|--------------------|--------------------|
| <code>0x400</code> | <code>0x120</code> |
| <code>0xF</code>   | <code>0x118</code> |
| <code>0x8</code>   | <code>0x110</code> |
| <code>0x10</code>  | <code>0x108</code> |
| <code>0x1</code>   | <code>0x100</code> |

```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```

# Example: lea vs. mov

## Registers

|      |              |
|------|--------------|
| %rax | <b>0x108</b> |
| %rbx | <b>0x10</b>  |
| %rcx | 0x2          |
| %rdx | 0x100        |
| %rdi | <b>0x100</b> |
| %rsi | <b>0x1</b>   |

## Memory

|       | Word Address |
|-------|--------------|
| 0x400 | 0x120        |
| 0xF   | 0x118        |
| 0x8   | 0x110        |
| 0x10  | 0x108        |
| 0x1   | 0x100        |

```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```

# Why does the compiler love `leaq`?

- Sometimes it's good for computing addresses
- Usually the compiler uses it to do math in fewer instructions
  - `addq` only adds a source and a destination, and overwrites destination
  - `leaq` adds up to two registers and an immediate, AND stores to a different register!

# Compiling Arithmetic Operations

```
int arith (long x, long y, long z) {  
    long t1 = x+y;  
    long t2 = z+t1;  
    long t3 = x+4;  
    long t4 = y * 48;  
    long t5 = t3 + t4;  
    long rval = t2 * t5;  
    .....  
}
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- **Don't expect a 1-1 mapping**

```
# rdi = x  
# rsi = y  
# rdx = z
```

# Compiling Arithmetic Operations

```
int arith (long x, long y, long z) {  
    long t1 = x+y;  
    long t2 = z+t1;  
    long t3 = x+4;  
    long t4 = y * 48;  
    long t5 = t3 + t4;  
    long rval = t2 * t5;  
    .....  
}
```

```
leaq (%rsi,%rdi),%rcx
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- **Don't expect a 1-1 mapping**

```
# rdi = x
```

```
# rsi = y
```

```
# rdx = z
```

```
# rcx = x+y (t1)
```

# Compiling Arithmetic Operations

```
int arith (long x, long y, long z) {  
    long t1 = x+y;  
    long t2 = z+t1;  
    long t3 = x+4;  
    long t4 = y * 48;  
    long t5 = t3 + t4;  
    long rval = t2 * t5;  
    .....  
}
```

```
leaq (%rsi,%rdi),%rcx  
leaq (%rsi,%rsi,2),%rsi  
salq $4,%rsi
```

```
# rdi = x  
# rsi = y  
# rdx = z  
# rcx = x+y (t1)  
# rsi = y + 2*y = 3*y  
# rsi = (3*y)*16 = 48*y (t4)
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- **Don't expect a 1-1 mapping**

# Compiling Arithmetic Operations

```
int arith (long x, long y, long z) {  
    long t1 = x+y;  
    long t2 = z+t1;  
    long t3 = x+4;  
    long t4 = y * 48;  
    long t5 = t3 + t4;  
    long rval = t2 * t5;  
    .....  
}
```

```
leaq (%rsi,%rdi),%rcx  
leaq (%rsi,%rsi,2),%rsi  
salq $4,%rsi  
addq %rdx,%rcx
```

```
# rdi = x  
# rsi = y  
# rdx = z  
# rcx = x+y (t1)  
# rsi = y + 2*y = 3*y  
# rsi = (3*y)*16 = 48*y (t4)  
# rcx = z+t1 (t2)
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- **Don't expect a 1-1 mapping**

# Compiling Arithmetic Operations

```
int arith (long x, long y, long z) {  
    long t1 = x+y;  
    long t2 = z+t1;  
    long t3 = x+4;  
    long t4 = y * 48;  
    long t5 = t3 + t4;  
    long rval = t2 * t5;  
    .....  
}
```

```
leaq (%rsi,%rdi),%rcx  
leaq (%rsi,%rsi,2),%rsi  
salq $4,%rsi  
addq %rdx,%rcx  
leaq 4(%rsi,%rdi),%rdi
```

```
# rdi = x  
# rsi = y  
# rdx = z  
# rcx = x+y (t1)  
# rsi = y + 2*y = 3*y  
# rsi = (3*y)*16 = 48*y (t4)  
# rcx = z+t1 (t2)  
# rdi = t4+x+4 (t5)
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- **Don't expect a 1-1 mapping**



# Compiling Arithmetic Operations

```
int arith (long x, long y, long z) {  
    long t1 = x+y;  
    long t2 = z+t1;  
    long t3 = x+4;  
    long t4 = y * 48;  
    long t5 = t3 + t4;  
    long rval = t2 * t5;  
    .....  
}
```

```
    leaq (%rsi,%rdi),%rcx  
    leaq (%rsi,%rsi,2),%rsi  
    salq $4,%rsi  
    addq %rdx,%rcx  
    leaq 4(%rsi,%rdi),%rdi  
    imulq %rcx,%rdi
```

```
# rdi = x  
# rsi = y  
# rdx = z  
# rcx = x+y (t1)  
# rsi = y + 2*y = 3*y  
# rsi = (3*y)*16 = 48*y (t4)  
# rcx = z+t1 (t2)  
# rdi = t4+x+4 (t5)  
# rdi = t2*t5 (rval)
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- **Don't expect a 1-1 mapping**

# Practice Question #1

| Address | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  |
|---------|----|----|----|----|----|----|----|----|
| 0x2000  | B5 | B7 | DC | ED | 7D | 59 | 08 | 93 |
| 0x2008  | 1D | 23 | 58 | 46 | 9C | 22 | 2F | 5D |
| 0x2010  | C6 | 83 | 75 | 00 | 41 | 19 | 87 | 1C |
| 0x2018  | 24 | 0C | 26 | AA | C7 | BD | 03 | 1E |
| 0x2020  | E3 | 00 | 00 | 00 | 00 | 00 | 00 | 00 |
| 0x2028  | 8B | DB | 66 | D7 | 21 | 23 | 6B | 99 |

| Register | Value  |
|----------|--------|
| %rax     | 0x2000 |
| %rbx     | 0x20   |
| %rcx     | 0x8    |

| Operation                            | Address Loaded | %rcx Value |
|--------------------------------------|----------------|------------|
| <code>movq (%rax, %rbx), %rcx</code> |                |            |

First, determine whether an address is loaded, and if so, which address?

# Practice Question #1

| Address | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  |
|---------|----|----|----|----|----|----|----|----|
| 0x2000  | B5 | B7 | DC | ED | 7D | 59 | 08 | 93 |
| 0x2008  | 1D | 23 | 58 | 46 | 9C | 22 | 2F | 5D |
| 0x2010  | C6 | 83 | 75 | 00 | 41 | 19 | 87 | 1C |
| 0x2018  | 24 | 0C | 26 | AA | C7 | BD | 03 | 1E |
| 0x2020  | E3 | 00 | 00 | 00 | 00 | 00 | 00 | 00 |
| 0x2028  | 8B | DB | 66 | D7 | 21 | 23 | 6B | 99 |

| Register | Value  |
|----------|--------|
| %rax     | 0x2000 |
| %rbx     | 0x20   |
| %rcx     | 0x8    |

| Operation                            | Address Loaded | %rcx Value |
|--------------------------------------|----------------|------------|
| <code>movq (%rax, %rbx), %rcx</code> | 0x2020         |            |

Second, determine the final value in `%rcx`

# Practice Question #1

| Address | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  |
|---------|----|----|----|----|----|----|----|----|
| 0x2000  | B5 | B7 | DC | ED | 7D | 59 | 08 | 93 |
| 0x2008  | 1D | 23 | 58 | 46 | 9C | 22 | 2F | 5D |
| 0x2010  | C6 | 83 | 75 | 00 | 41 | 19 | 87 | 1C |
| 0x2018  | 24 | 0C | 26 | AA | C7 | BD | 03 | 1E |
| 0x2020  | E3 | 00 | 00 | 00 | 00 | 00 | 00 | 00 |
| 0x2028  | 8B | DB | 66 | D7 | 21 | 23 | 6B | 99 |

| Register | Value  |
|----------|--------|
| %rax     | 0x2000 |
| %rbx     | 0x20   |
| %rcx     | 0x8    |

| Operation               | Address Loaded | %rcx Value |
|-------------------------|----------------|------------|
| movq (%rax, %rbx), %rcx | 0x2020         | 0xE3       |

# Practice Question #2

| Address | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  |
|---------|----|----|----|----|----|----|----|----|
| 0x2000  | B5 | B7 | DC | ED | 7D | 59 | 08 | 93 |
| 0x2008  | 1D | 23 | 58 | 46 | 9C | 22 | 2F | 5D |
| 0x2010  | C6 | 83 | 75 | 00 | 41 | 19 | 87 | 1C |
| 0x2018  | 24 | 0C | 26 | AA | C7 | BD | 03 | 1E |
| 0x2020  | E3 | 00 | 00 | 00 | 00 | 00 | 00 | 00 |
| 0x2028  | 8B | DB | 66 | D7 | 21 | 23 | 6B | 99 |

| Register | Value  |
|----------|--------|
| %rax     | 0x2000 |
| %rbx     | 0x20   |
| %rcx     | 0x8    |

| Operation                            | Address Loaded | %rcx Value |
|--------------------------------------|----------------|------------|
| <code>leaq (%rax, %rbx), %rcx</code> |                |            |

First, determine whether an address is loaded, and if so, which address?

# Practice Question #2

| Address | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  |
|---------|----|----|----|----|----|----|----|----|
| 0x2000  | B5 | B7 | DC | ED | 7D | 59 | 08 | 93 |
| 0x2008  | 1D | 23 | 58 | 46 | 9C | 22 | 2F | 5D |
| 0x2010  | C6 | 83 | 75 | 00 | 41 | 19 | 87 | 1C |
| 0x2018  | 24 | 0C | 26 | AA | C7 | BD | 03 | 1E |
| 0x2020  | E3 | 00 | 00 | 00 | 00 | 00 | 00 | 00 |
| 0x2028  | 8B | DB | 66 | D7 | 21 | 23 | 6B | 99 |

| Register | Value  |
|----------|--------|
| %rax     | 0x2000 |
| %rbx     | 0x20   |
| %rcx     | 0x8    |

| Operation                            | Address Loaded | %rcx Value |
|--------------------------------------|----------------|------------|
| <code>leaq (%rax, %rbx), %rcx</code> | None           |            |

Second, determine the final value in `%rcx`

# Practice Question #2

| Address | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  |
|---------|----|----|----|----|----|----|----|----|
| 0x2000  | B5 | B7 | DC | ED | 7D | 59 | 08 | 93 |
| 0x2008  | 1D | 23 | 58 | 46 | 9C | 22 | 2F | 5D |
| 0x2010  | C6 | 83 | 75 | 00 | 41 | 19 | 87 | 1C |
| 0x2018  | 24 | 0C | 26 | AA | C7 | BD | 03 | 1E |
| 0x2020  | E3 | 00 | 00 | 00 | 00 | 00 | 00 | 00 |
| 0x2028  | 8B | DB | 66 | D7 | 21 | 23 | 6B | 99 |

| Register | Value  |
|----------|--------|
| %rax     | 0x2000 |
| %rbx     | 0x20   |
| %rcx     | 0x8    |

| Operation                            | Address Loaded | %rcx Value |
|--------------------------------------|----------------|------------|
| <code>leaq (%rax, %rbx), %rcx</code> | None           | 0x2020     |

# Break + Say hi to your neighbors

- Things to share
  - Name
  - Major
  - One of the following
    - Favorite Candy
    - Favorite Pokemon
    - Favorite Emoji



# Break + Say hi to your neighbors

- Things to share
  - Name -Branden
  - Major -Electrical and Computer Engineering, and Computer Science
  - One of the following
    - Favorite Candy - Twix
    - Favorite Pokemon - Eevee
    - Favorite Emoji - 🍷

# Outline

- Arithmetic Instructions
- Special Cases
  - Non 64-bit Data
  - Load Effective Address
- **Condition Codes**
- Viewing x86-64 Assembly

# What can instructions do?

- Move data: ✓
- Arithmetic: ✓
- Transfer control: **X**
  - Instead of executing next instruction, go somewhere else
- Let's back out. Why do we want that?

```
if (x > y)
    result = x-y;
else
    result = y-x;
```

```
while (x > y)
    result = x-y;
return result;
```

- Sometimes we want to go from the red code to the green code
- But the blue code is what's next!
- Need to transfer control! Execute an instruction that is not the next one
- And **conditionally**, too! (i.e., based on a condition)

# Condition codes

- Control is mediated via *Condition codes*
  - single-bit registers that record answers to questions about values
  - E.g., Is value x greater than value y? Are they equal? Is their sum even?
  - Let's keep "question" abstract for now. We'll see the details in a bit.
- **Terminology:**
  - a bit is ***set*** if it is 1
  - a bit is ***cleared*** (or ***reset***) if it is 0

# Conditionals at the machine level

- At machine level, conditional operations are a 2-step process:
  - Perform an operation that **sets** or **clears** condition codes (ask questions)
  - Then **observe** which condition codes are set, do the operation (or not)
- Can express Boolean operations, conditionals, loops, etc.
  - We will see the first today, and more control next lecture
- So now we need three things:
  1. Instructions that compare values and set condition codes
  2. Instructions that observe condition codes and do something (or not)
  3. A set of actual condition codes (what questions do we track answers to?)

# Two-Step Conditional Process: Boolean Operations

- Lots of new pieces
- Lets give an example first, then learn more about each
  - Translate C code on right into assembly
  - We'll do this in the next steps

```
bool gt (int x, int y)
{
    return x > y;
}
```

| Register | Use(s)       |
|----------|--------------|
| %rdi     | Argument x   |
| %rsi     | Argument y   |
| %rax     | Return value |

```
cmpq    %rsi, %rdi    # Compare x:y
setg    %al           # Set when x > y (i.e., %rdi > %rsi)
ret
```

# Two-Step Conditional Process: Boolean Operations

- Step 1, `cmpq`: compare quad words
  - *compare* the values in `%rsi` and `%rdi`, keep track of *all* you can learn, and set the relevant condition codes
  - Are the two equal? Set the condition codes that records they were equal
  - Was the right one greater? Or less? Etc.
  - We don't know yet which answer we are going to need! So just save them all.

```
bool gt (int x, int y)
{
    return x > y;
}
```

| Register          | Use(s)       |
|-------------------|--------------|
| <code>%rdi</code> | Argument x   |
| <code>%rsi</code> | Argument y   |
| <code>%rax</code> | Return value |

The diagram shows assembly code with callouts for registers `y` and `x`. A thick black arrow points to the first instruction. The code is as follows:

```
cmpq    %rsi, %rdi    # Compare x:y
setg    %al           # Set when x > y (i.e., %rdi > %rsi)
ret
```

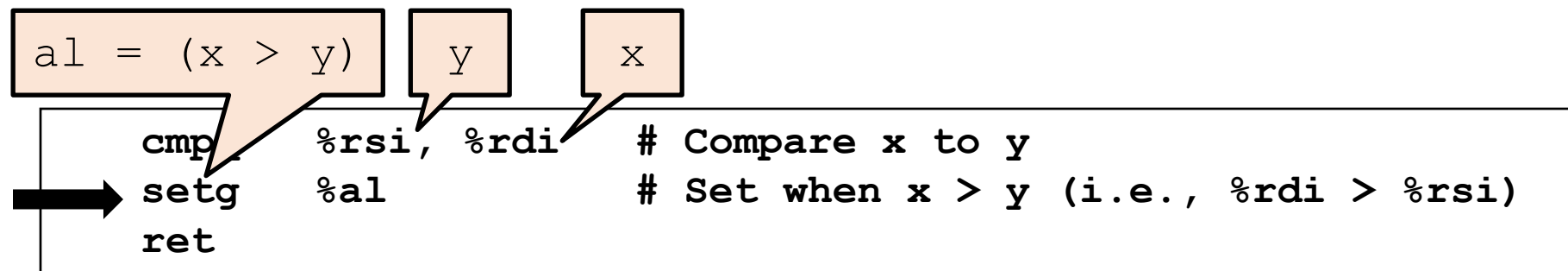
Callout boxes labeled 'y' and 'x' point to `%rsi` and `%rdi` respectively in the `cmpq` instruction.

# Two-Step Conditional Process: Boolean Operations

- Step 2, **setX**: set destination register to 1 if condition is met
  - **setg** = set if the 2<sup>nd</sup> operand is *greater than* the 1<sup>st</sup> (careful about the order!)
    - There's also **setl** for less than, etc.
  - Reads the condition codes that encodes the answer to that question
  - Set the 1-byte register **%a1** to 1 if true

```
bool gt (int x, int y)
{
    return x > y;
}
```

| Register | Use(s)       |
|----------|--------------|
| %rdi     | Argument x   |
| %rsi     | Argument y   |
| %rax     | Return value |





# Step 1: Setting condition codes

- Analogy: Asking ALL the possible questions at once
  - And recording the answers
  - We don't know yet which question is the one we care about!
- Done in one of two ways
  - **Implicitly**: all\* arithmetic instructions set (and reset) condition codes in addition to producing a result
    - \*except `leaq`; it's not "officially" an arithmetic instruction
  - **Explicitly**: by instructions whose sole purpose is to set condition codes
    - E.g., `cmprq`
    - They don't actually produce results (in registers or memory)
- Condition codes are left unchanged by other operations (such as `mov`)

# What are the Condition Codes?

- Condition codes on x86
  - **CF** Carry Flag (for unsigned)
  - **ZF** Zero Flag
  - **PF** Parity Flag
  - **SF** Sign Flag (for signed)
  - **OF** Overflow Flag (for signed)
- Not an arbitrary set! By combining them, can keep track of answers to many useful questions! (We'll see exactly which in a bit.)

# Implicitly Setting Condition Codes

**CF** (Carry)   **SF** (Sign)   **ZF** (Zero)   **OF** (Overflow)   **PF** (Parity)

- Set (or reset) based on the result of arithmetic operations

Example: `addq Src, Dest`   # C-analog: `t = a+b`

- **ZF set** if `t == 0`
- **SF set** if `t < 0` (as signed encoding)
- **CF set** if carry out from most significant bit (unsigned overflow)  
also CF takes the value of the last bit shifted (left or right)
- **OF set** if twos-complement (signed) overflow (pos/neg overflow)  
`(a>0 && b>0 && t<0) || (a<0 && b<0 && t>=0)`  
also, set if a 1-bit shift operation changes the sign of the result
- **PF set** if `t` has an even number of 1 bits

# Explicitly Setting Condition Codes: Compare

- `cmp{b,w,l,q} Src2, Src1`
- `cmpq b, a` computes  $t = a - b$ , then throws away the result
  - And sets condition codes along the way, like `subq` would!
  - Follows the rules we saw on the previous slide for arithmetic instructions
  - **Beware the order of the `cmp` operands!**
- Use cases
  - **ZF set** if  $a == b$
  - **SF set** if  $(a - b) < 0$  (as signed), i.e.,  $b > a$  in a signed comparison!
  - **CF and OF** used mostly in combinations with others (see in a few slides)

# Explicitly Setting Condition Codes: Test

- `test{b,w,l,q} Src2,Src1`
- `testq b,a` computes `t = a&b`, then throws away the result!
  - And sets condition codes like `andq` would (order doesn't matter here)
  - So again, same rules as arithmetic instructions
- Use cases
  - **ZF set** when `a&b == 0`, i.e., `a` and `b` have no bits in common
  - **SF set** when `a&b < 0`
- Useful when doing bit masking
  - E.g., `x & 0x1`, to know whether `x` is even or odd
  - If the result of the `&` is 0, it's even, if 1, it's odd

## Step 2: Reading Condition Codes

- Cannot read condition codes directly; instead observe via instructions
  - And generally observe *combinations* of condition codes, not individual ones
- Example: the **setX** family of instructions
  - Write single-byte destination register based on combinations of condition codes
    - **set{e, ne, s, ...} D** where D is a 1-byte register
    - Example: **sete %a1**
      - Means: **%a1=1** if flag ZF is set, **%a1=0** otherwise

# Using condition codes for comparison

- `setle` – Less than or equal (signed)
  - Combination of condition codes:  $(SF \wedge OF) \vee ZF$
  - SF - Sign Flag (true if negative)
  - OF – Overflow Flag (true if signed overflow occurred)
  - ZF – Zero Flag (true if result is zero)
- All of the combos expect to be run after a `cmp src, dst`
  - `dst <= src` (runs `dst-src`)
    - If:
      - The result is zero – `src` and `dst` were equal
    - OR if one but not both:
      - The result is negative (and didn't overflow) – `src` was larger than `dst`
      - The result overflowed (and is positive) – `dst` is negative, `src` is positive

# Condition codes combinations

| SetX               | Description               | Condition                            |
|--------------------|---------------------------|--------------------------------------|
| <code>sete</code>  | Equal / Zero              | $ZF$                                 |
| <code>setne</code> | Not Equal / Not Zero      | $\sim ZF$                            |
| <code>sets</code>  | Negative                  | $SF$                                 |
| <code>setns</code> | Nonnegative               | $\sim SF$                            |
| <code>setg</code>  | Greater (Signed)          | $\sim (SF \wedge OF) \ \& \ \sim ZF$ |
| <code>setge</code> | Greater or Equal (Signed) | $\sim (SF \wedge OF)$                |
| <code>setl</code>  | Less (Signed)             | $(SF \wedge OF)$                     |
| <code>setle</code> | Less or Equal (Signed)    | $(SF \wedge OF) \   \ ZF$            |
| <code>seta</code>  | Above (unsigned)          | $\sim CF \ \& \ \sim ZF$             |
| <code>setb</code>  | Below (unsigned)          | $CF$                                 |

Note: suffixes do not indicate operand sizes, but rather conditions

These same suffixes will come back when we see other instructions that read condition codes.

Expect to be run after a **cmp**



## Step 2: Reading Condition Codes

- `setX` (and others) read the current state of condition codes
  - Whatever it is, and whichever instruction changed it last
- So when you see (for example) `setne`, work backwards!
  - Look at previous instructions, to find the last one to change conditions
  - Then you'll know the two values that were compared
  - Ignore instructions that don't touch condition codes (like moves)
- Usually you'll see a `cmpX` (or `testX`, or arithmetic) right before
  - But not always, so know what to do in general

# What do you need to know?

- 90%+ of the time
  - `cmp` instruction followed by `setX` instruction (or a jump, next lecture)
  - Don't have to think about condition codes at all!
  - Think of as `dst X src`
    - `dst <= src`      or      `dst != src`      etc.
- 10% or less of the time
  - Arbitrary arithmetic instruction sets the condition codes
    - Or `testq` sets the condition codes
  - Followed by a `setX` or branch (next lecture)
  - And you actually have to think about which condition codes are set to figure out what the assembly is doing, which can be challenging

# Outline

- Arithmetic Instructions
- Special Cases
  - Non 64-bit Data
  - Load Effective Address
- Condition Codes
- **Viewing x86-64 Assembly**

# How to Get Your Hands on Assembly

- From C source code, using a compiler
  - `gcc -O1 -S sum.c`
    - Produces file `sum.s`
  - **Warning:** May get very different results on different machines due to different versions of gcc and different compiler settings

## C Code: sum.c

```
long plus(long x, long y);  
  
void sum(long x, long y,  
         long *dest)  
{  
    long t = plus(x, y);  
    *dest = t;  
}
```

## Generated x86-64 assembly: sum.s

```
sum:  
    pushq    %rbx  
    movq    %rdx, %rbx  
    call   plus  
    movq    %rax, (%rbx)  
    popq    %rbx  
    ret
```

# How to Get Your Hands on Assembly

- From machine code, using a disassembler
  - `objdump -d sum.o`
  - Within the gdb Debugger

```
linux> gdb prog
(gdb) disassemble sum
```

    - gdb tutorial coming soon!
  - **Warning:** Disassemblers are approximate; some information is lost during translation from assembly to machine code
    - Label names are lost, what is just data (vs code) is lost, etc.
- Useful if you don't have the source

```
0000000000400595 <sum>:
 400595: 53                push   %rbx
 400596: 48 89 d3          mov    %rdx,%rbx
 400599: e8 f2 ff ff ff   callq 400590 <plus>
 40059e: 48 89 03          mov    %rax,(%rbx)
 4005a1: 5b                pop    %rbx
 4005a2: c3                retq
```

# Godbolt

Ignore section labeled:  
“\_dl\_relocate\_static\_pie”

Play around with this to  
try stuff on your own

<https://godbolt.org/>

The screenshot displays the Godbolt Compiler Explorer interface. The left pane shows C source code with three functions: `square`, `add_inputs_plus_two`, and `check_greater`. The right pane shows the assembly output for these functions, with labels like `_dl_relocate_static_pie`, `square:`, `add_inputs_plus_two:`, and `check_greater:`. The assembly instructions include `imul`, `mov`, `retq`, `lea`, `cmp`, and `setg`. The interface also features a top navigation bar with 'COMPILER EXPLORER' logo, 'Listen to the Cpp.chat podcast' button, and various utility buttons like 'Sponsors', 'Share', and 'Policies'.

```
1 // Type your code here, or load an example.
2 int square(int num) {
3     return num * num;
4 }
5
6
7 int add_inputs_plus_two(int a, int b) {
8     return a+b+2;
9 }
10
11
12 char check_greater(int a, int b) {
13     return (a > b);
14 }
```

```
401050 endbr64
c3
401054 retq
66 2e 0f 1f 84 00 00 00 00 00
401055 nopw %cs:0x0(%rax,%rax,1)
90
40105f nop
square:
0f af ff
401102 imul %edi,%edi
89 f8
401105 mov %edi,%eax
c3
401107 retq
add_inputs_plus_two:
8d 44 37 02
401108 lea 0x2(%rdi,%rsi,1),%eax
c3
40110c retq
check_greater:
39 f7
40110d cmp %esi,%edi
0f 9f c0
40110f setg %al
c3
401112 retq
```

- Godbolt example!

# Outline

- Arithmetic Instructions
- Special Cases
  - Non 64-bit Data
  - Load Effective Address
- Condition Codes
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