Lecture 02 Data Representations

CS213 – Intro to Computer Systems Branden Ghena – Winter 2024

Slides adapted from: St-Amour, Hardavellas, Bustamente (Northwestern), Bryant, O'Hallaron (CMU), Garcia, Weaver (UC Berkeley)

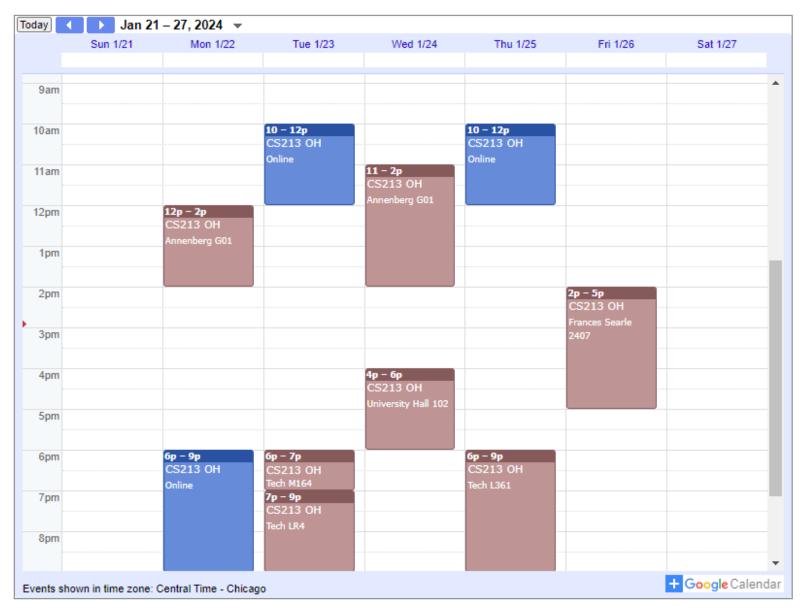
Northwestern

Announcements

- Homework 1 will be posted sometime later today
 - Practice problems on binary-to-hex-to-decimal conversion, integer encodings, and memory
 - Today's lecture will finish the content you need for it
 - Due Tuesday January 16th
 - You'll submit to Gradescope, which I'll add you all too as well

Office Hours

- Start on Wednesday of this week
- Variety of times, with most in-person but some online
- Depending on slot, 2-6 staff members available to help people
- Help queue signup and status on Canvas homepage



Today's Goals

Review of binary and hexadecimal

• Discuss data representation in memory

- Explore data representations
 - Integers, signed and unsigned
 - Different bit widths
 - Translating between encoding schemes
 - Other encodings besides integers

Outline

- Binary and Hex
- Memory
- Encoding
- Integer Encodings
 - Signed Integers
 - Converting Sign
 - Converting Length
- Other encodings

Positional Numbering Systems

- The position of a *numeral* (e.g., digit) determines its contribution to the overall number
 - Makes arithmetic simple (compared to, say, roman numerals)
 - Any number has one canonical representation

- Example: base 10
 - $10456_{10} = 1*10^4 + 0*10^3 + 4*10^2 + 5*10^1 + 6*10^0$
 - Usually, we leave out the zeros:
 - $1*10^4$ + $4*10^2$ + $5*10^1$ + $6*10^0$

Practice: Base 2

- Translate 0b10111 to decimal (0b means binary)
 - 1*16 + 0*8 + 1*4 + 1*2 + 1*1
 - 16 + 4 + 2 + 1
 - 23

- Translate decimal 40 to binary
 - 32 + 8
 - 1*32 + 0*16 + 1*8 + 0*4 + 0*2 + 0*1
 - 0b101000

Base 16: Hexadecimal

- Writing long sequences of 0s and 1s is tedious and error-prone
 - And takes up a lot of space on a page!
- So we'll often use base 16 (also called hexadecimal)
- Base 2 = 2 symbols (0, 1) Base 10 = 10 symbols (0-9) Base 16, need 16 symbols
 - Use letters A-F once we run out of decimal digits
- Example: 0x3A (0x means hexadecimal)

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
Α	10	1010
В	11	1011
С	12	1100
D	13	1101
E	14	1110
F	15	1111

Hex example

- Convert decimal 165 to hex (first convert to binary)
- Decimal to binary
 - 165
 - 128 + 32 + 4 + 1
 - 1*128 + 0*64 + 1*32 + 0*16 + 0*8 + 1*4 + 0*2 + 1*1
 - 0b10100101
- Binary to hex
 - 0b1010 0101
 - 0xA5

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
Α	10	1010
В	11	1011
С	12	1100
D	13	1101
Ε	14	1110
F	15	1111

Specific bit widths

- Since computers are hardware, cannot have arbitrary bit lengths
 - Must be *some* specific number of bits
 - We'll say "this is a 16-bit number" or this is a "9-bit number"
- What if the number of bits isn't divisible by four, can it still be hex?
 - Yes! All non-existent bits MUST be zero
- Example: translate 0x35 to a 6-bit binary number
 - 0b0011 0101 -> 0b11 0101
 - If it had been 0x75 (0b111 0101) writing as a 6-bit binary number would be impossible (converting could happen, but we'd have overflow)

More bit-width examples

- Convert 0b11 to hexadecimal
 - 0x3

- How many bits is 0x3?
 - MUST be at least 2 bits
 - Could be more though: 4-bit, or 64-bit, or as many zeros as you want

Outline

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- Integer Encodings
 - Signed Integers
 - Converting Sign
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- Other encodings

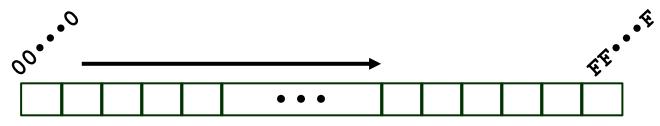
Bytes

- A single bit doesn't hold much information
 - Only two possible values: 0 and 1
 - So we'll typically work with larger groups of bits
- For convenience, we'll refer to groups of 8 bits as *bytes*
 - And usually work with multiples of 8 bits at a time
 - Conveniently, 8 bits = 2 hexits
- Some examples
 - 1 byte: 0b01100111 = 0x67
 - 2 bytes: $11000100 00101111_2 = 0xC42F$

"0b" prefix = it's in binary "0x" prefix = it's in hex

Byte-oriented memory organization

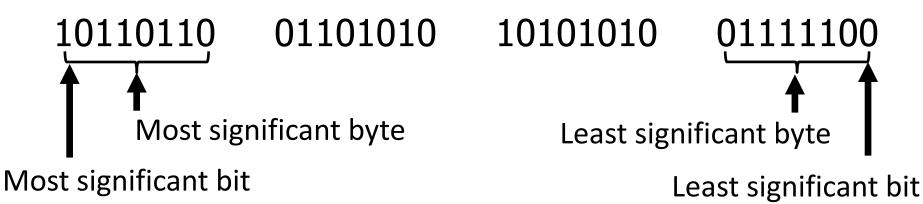
- We've seen how sequences of bits can express numbers
 - And how we usually work with groups of 8 bits (bytes) for convenience
 - Variables are almost always some multiple number of bytes (1 byte, 2 bytes, 8 bytes, etc.)
- In a computer system, bytes can be stored in memory
 - Conceptually, memory is a very large array of bytes
 - Each byte has its own address (≈ pointer)



- Compiler + run-time system control allocation
 - Where different program objects should be stored
 - Multiple mechanisms, each with its own region: static, stack, and heap

Most/least significant bits/bytes

- When working with sequences of bits (or sequences of bytes), need to be able to talk about specific bits (bytes)
 - Most Significant bit (MSb) and Most Significant Byte (MSB)
 - Have the largest possible contribution to numeric value
 - Leftmost when writing out the binary sequence
 - Least Significant bit (LSb) and Least Significant Byte (LSB)
 - Have the smallest possible contribution to numeric value
 - Rightmost when writing out the binary sequence



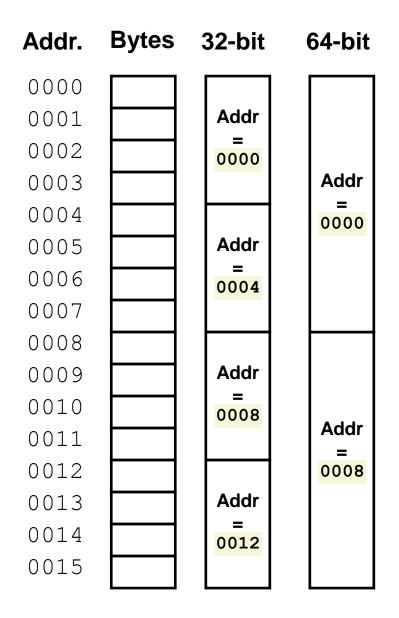
Addressing and byte ordering

- For data that spans multiple bytes, need to agree on two things
 - 1. What should be the address of the object? (each byte has its own!)
 - And by extension, given an address, how do we find the relevant bytes (same question!)
 - 2. How should we order the bytes in memory?
 - Do we put the most or least significant byte at the first address?

There isn't always one correct answer

- Different systems can pick different answers! (mostly for 2nd Q)
 - Very nice illustration of two overarching principles in systems: You need to know the specifics of the system you're using!
 - Many questions don't really have right or wrong answers!
 - Instead, they have tradeoffs. What the "right" answer is depends on context!
 - Different answers across systems is perfectly fine
 - But all the parts of a given system must agree with each other!

- 1. Addressing data in memory
- All addresses refer to one or more bytes
 Never bits
- For multi-byte objects, the lowest address refers to the entire object
 - Addresses of successive objects differ by 4 (32-bit) or 8 (64-bit)
- Systems pretty much universally use the address of the first byte as the address for the whole object
 - I'm not aware of any system that does otherwise
 - But there could be some weirdo systems out there (or historically)



2. Byte ordering

- How to order bytes within a multi-byte object in memory
 - Only relevant when working with data larger than a byte!
- Conventions

• Example

- Big Endian: Computer Networks, various historical computer systems
 - Most significant byte has lowest address (comes first)
- Little Endian: Intel (x86, x86-64), ARM, other modern computer systems

Big Endian

• Least significant byte has lowest address (comes first)

 Increasing memory addresses

 0x100
 0x101
 0x102
 0x103

 01
 23
 45
 67

• Address of that data is **0x100**

• 4-byte piece of data: 0x01234567

ittle E	Endian	0x100	0x101	0x102	0x103	
		67	45	23	01	

- Assume memory is Little Endian
 - So the Least Significant Byte comes first
- 1. What is the four-byte value at 0x2010?

2. What is the two-byte value at 0x2014?

3. What is the one-byte value at 0x2016?

Address	Value
0x2010	0x37
0x2011	0x1A
0x2012	0xBE
0x2013	0x98
0x2014	0x0C
0x2015	0x80
0x2016	0x42

- Assume memory is Little Endian
 - So the Least Significant Byte comes first
- What is the four-byte value at 0x2010?
 0x98BE1A37
- 2. What is the two-byte value at 0x2014?**0x800C**
- 3. What is the one-byte value at 0x2016?0x42

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- Assume memory is Little Endian
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- Change: assume memory is Big Endian
 - So the Most Significant Byte comes first
- What is the four-byte value at 0x2010?
 0x371ABE98
- 2. What is the two-byte value at 0x2014?**0x0C80**
- 3. What is the one-byte value at 0x2016?

0x42

Note: endianness doesn't affect one-byte values!

Address	Value
0x2010	0x37
0x2011	0x1A
0x2012	0xBE
0x2013	0x98
0x2014	0x0C
0x2015	0x80
0x2016	0x42

Tables of memory

Address	0	1	2	3	4	5	6	7
0x1040	2E	E2	BD	62	EF	AØ	CD	93
0x1048	A4	75	61	2F	ØF	DB	64	A4
0x1050	54	7A	F2	60	6E	47	BØ	92
0x1058	DA	72	8F	A8	E5	15	18	CE
0x1060	86	BF	6A	6A	92	99	CF	6C

- Method of displaying large chunks of memory
 - 8 bytes per row (in this example)
 - Data values in hexadecimal
- Memory addresses labeled on the left and byte offset on the top
 - Also in hexadecimal

Tables of memory

Address	0	1	2	3	4	5	6	7
0x1040	2E	E2	BD	62	EF	AØ	CD	93
0x1048	A4	75	61	2F	ØF	DB	64	A4
0x1050	54	7A	F2	60	6E	47	BØ	92
0x1058	DA	72	8F	A8	E5	15	18	CE
0x1060	86	BF	6A	6A	92	99	CF	6C

- To find an address: deconstruct into:
 - base address (left) + offset (top)
- Remember: addresses are in hexadecimal!
 - 0x1048+2 = 0x104A

Practice: Tables of memory

Address	0	1	2	3	4	5	6	7
0x1040	2E	E2	BD	62	EF	AØ	CD	93
0x1048	A4	75	61	2F	ØF	DB	64	A4
0x1050	54	7A	F2	60	6E	47	BØ	92
0x1058	DA	72	8F	A8	E5	15	18	CE
0x1060	86	BF	6A	6A	92	99	CF	6C

- What value is at address 0x1050?
 - 0x54 (0x1050 + 0)
- What value is at address 0x105F?
 - 0xCE (0x1058 + 7)

Outline

- Binary and Hex
- Memory
- Encoding
- Integer Encodings
 - Signed Integers
 - Converting Sign
 - Converting Length
- Other encodings

Big Idea: What do bits and bytes *mean* in a system?

- The answer is: it depends!
- Depending on the context, the bits 11000011 could mean
 - The number 195
 - The number -61
 - The number -19/16
 - The character ` |'
 - The ret x86 instruction
- You have to know the context to make sense of any bits you have!
 - Looking at the same bits in different contexts can lead to interesting results
 - Information = bits + context!
- An *encoding* is a set of rules that gives meaning to bits

An example encoding: ASCII characters

- ASCII = American Standard Code for Information Interchange
 - Standard dating from the 60s
- Maps 8-bit* bit patterns to characters
 - (* the standard is actually 7-bit, leaving the 8th bit unused)
 - We already know how to go from sequences of bits (base 2) to integers
 - Need to take one more step, and interpret these integers as characters
- Examples
 - $0100\ 0001_2 = 0x41 = 65_{10} = `A'$
 - $0100\ 0010_2^- = 0x42 = 66_{10}^{-10} = `B'$
 - $0011\ 0000_2 = 0x30 = 48_{10} = 0'$
 - $0011\ 0001_2 = 0x31 = 49_{10} = 1'$
- Reference: https://www.asciitable.com/

E II	Dec HxOct Char Dec	ec Hx Oct Html Chr [Dec Hx Oct Html Chr Dec Hx Oct Html Chr
Full	0 0 000 NUL (null) 32	2 20 040 Space	64 40 100 «#64; 0 96 60 140 «#96; `
	1 1 001 SOH (start of heading) 33	3 21 041 ! !	65 41 101 «#65; A 97 61 141 «#97; a
ASCII		4 22 042 " "	66 42 102 «#66; B 98 62 142 «#98; b
		5 23 043 # #	67 43 103 «#67; C 99 63 143 «#99; C
table		6 24 044 \$ \$	68 44 104 «#68; D 100 64 144 «#100; d
Capic		7 25 045 % 🗞	69 45 105 «#69; E 101 65 145 «#101; e
		8 26 046 & <u>«</u>	70 46 106 «#70; F 102 66 146 «#102; f
Values listed		9 27 047 ' ' 0 28 050 ((71 47 107 G G 103 67 147 g g 72 48 110 H H 104 68 150 h h
-		1 29 051 6#41;)	73 49 111 «#73; I 104 66 150 «#104; II 73 49 111 «#73; I 105 69 151 «#105; i
in:		2 2A 052 * *	74 4A 112 «#74; J 106 6A 152 «#106; j
		3 2B 053 + +	75 4B 113 K K 107 6B 153 k k
Docimal		4 2C 054 «#44;	76 4C 114 «#76; L 108 6C 154 «#108; L
Dec imal		5 2D 055 «#45; -	77 4D 115 «#77; M 109 6D 155 «#109; M
		6 2E 056 . .	78 4E 116 «#78; N 110 6E 156 «#110; n
Hex adecimal		7 2F 057 / /	79 4F 117 «#79; 0 111 6F 157 «#111; 0
	16 10 020 DLE (data link escape) 48	8 30 060 «#48; 0	80 50 120 «#80; P 112 70 160 «#112; P
	17 11 021 DC1 (device control 1) 49	9 31 061 «#49; 1	81 51 121 «#81; Q 113 71 161 «#113; q
Oct al	18 12 022 DC2 (device control 2) 50	0 32 062 2 <mark>2</mark>	82 52 122 «#82; R 114 72 162 «#114; r
		1 33 063 3 3	83 53 123 «#83; S 115 73 163 «#115; S
HTML		2 34 064 4 4	84 54 124 T T 116 74 164 t t
		3 35 065 «#53; <mark>5</mark>	85 55 125 «#85; U 117 75 165 «#117; u
		4 36 066 «#54; <mark>6</mark>	86 56 126 ∝#86; V 118 76 166 ∝#118; V
Char acter			87 57 127 ≪#87; ₩ 119 77 167 ≪#119; ₩
		I	88 58 130 «#88; X 120 78 170 «#120; X
		7 39 071 9 9	89 59 131 «#89; Y 121 79 171 «#121; Y
		8 3A 072 : :	90 5A 132 Z Z 122 7A 172 z Z
		9 3B 073 ; ; 0 3C 074 < <	91 5B 133 [[123 7B 173 { { 92 5C 134 \ \ 124 7C 174
	· - · ·	1 3D 075 = =	93 5D 135 «#93;] 125 7D 175 «#125; }
		2 3E 076 >>	94 5E 136 «#94; ^ 126 7E 176 «#126; ~
		I	95 5F 137 _ _ 127 7F 177 DEL

Source: www.LookupTables.com

Encodings are just determined by people

- There's no inherent **truth** in the design of an encoding
 - Although some encodings are nice or annoying for various reasons
 - Example: it's nice in ASCII that letters are in alphabetical order

- You could come up with an entirely new way of encoding characters
 - The hard part would be getting everyone else to agree to use it

Open Question + Break

What things might we want to encode?

Open Question + Break

What things might we want to encode?

- Numbers
 - Signed and unsigned integers
 - Real numbers
 - Mathematical symbols: $\infty~\pi$
- Language
 - Characters in various different languages ΩΛ心서北
 - Emoji 🚱 😥 🗑 😰 🕼 🥵 🌮 🎘 📎
- Colors, Playing Cards, User Actions, anything!

Outline

- Binary and Hex
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Integer Encodings

- Signed Integers
- Converting Sign
- Converting Length
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Integer types in C

- C type provides both size and encoding rules
- Integer types in C come in two flavors
 - Signed: short, signed short, int, long, ...
 - Unsigned: unsigned char, unsigned short, unsigned int, ...
- And in multiple different sizes
 - 1 byte: signed char, unsigned char
 - 2 bytes: short, unsigned short
 - 4 bytes: int, unsigned int
 - Etc.

Sizes of C types are system dependent

- Portability
 - Some programmers assume an int can be used to store a pointer
 - OK for most 32-bit machines, but fails for 64-bit machines!
- How I program
 - Use fixed width integer types from <stdint.h>
 - int8_t, int16_t, int32_t
 - uint8_t, uint16_t, uint32_t

C Data Type	Intel IA32	x86-64	C Standard* (C99)
char	1	1	≥1
short	2	2	≥2
int	4	4	≥2
long	4	8	≥4
long long	8	8	≥8
float	4	4	
double	8	8	
pointer	4	8	Widths for data, code pointers may differ!

CS213 uses this

Expressing C types in bits

- Two families of encodings to express integers using bits
 - **Unsigned** encoding for unsigned integers
 - *Two's complement* encoding for signed integers
- Each encoding will use a fixed size (# of bits)
 - For a given machine
 - Size + encoding family determine which C type we're representing
 - Reverse is also true: a C type specifies both size and encoding
 - Fixed size is because computers are finite!

Unsigned integer encoding

- Just write out the number in binary
 - Works for 0 and all positive integers
- Example: encode 104_{10} as an **unsigned** 8-bit integer
 - $104_{10} = 0 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$ $\Rightarrow 01101000$
 - \Rightarrow 0x68

$$B2U(X) = \sum_{i=0}^{w-1} x_i \cdot 2^i$$
(Binary To Unsigned)

Bounds of unsigned integers

- For a fixed width *w*, a limited range of integers can be expressed
 - Smallest value (we will call *UMin*):
 - all 0s bit pattern: 000...0, value of 0
 - Largest value (we will call **UMax**):
 - all 1s bit pattern: 111...1, value of $2^w 1$
 - $2^{w} 1 = 1 \times 2^{w-1} + 1 \times 2^{w-2} + \dots + 1 \times 2^{1} + 1 \times 2^{0} = 11111\dots$
- Maximum 8-bit number = $2^{8}-1 = 256-1 = 255$

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Encoding signed integers

- What's different about representing a signed number?
 - It can be negative!
- So, we're going to have to somehow represent values that are negative and positive

- There are actually many different encodings capable of doing this
 - This is when that "nice encoding" versus "annoying encoding" matters

Doesn't work: attempting signed encoding

• Goal: encode integers that can be positive or negative

- First attempt: we can use the most significant bit for sign
 - "Sign-and-magnitude" encoding
 - In 8-bits:
 - +4 = 00000100+127 = 01111111+0 = 00000000• -4 = 10000100-127 = 11111111-0 = 10000000
- Annoying problem: we have two representations of zero!
- Also annoying: hardware to do math with signed and unsigned numbers gets complicated...

Does work: Two's complement encoding

- Bad news: need to make the encoding more complicated
- Good news: it will actually work
- Plan:
 - Start with unsigned encoding, but make ONLY the largest power negative
 - Example: for 8 bits, most significant bit is worth -2⁷ not +2⁷ (other bits are still positive)
- To encode a negative integer
 - First, set the most significant bit to 1 to start with a big negative number
 - Then, add positive powers of 2 (the other bits) to "get back" to number we want
- Example: encode -6 as a 4-bit two's complement integer

• $-6_{10} = 1 \times -2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^1 \Rightarrow 0b1010 \Rightarrow 0xa$

Two's complement examples

- Encode -100 as an 8-bit two's complement number
 - $-100_{10} = 1 \times -2^7 + 0 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$

-128 + 0 + 0 + 16 + 8 + 4 + 0 + 0 Problem becomes: encode + 28 as a 7-bit unsigned number

- $-100_{10} = 0b10011100 = 0x9C$
- **Shortcut:** determine positive version of number, flip all the bits, and add one
 - $100_{10} = 0b01100100$
 - Flipped = 0b10011011
 - Plus 1 = 0b10011100 = 0x9C We'll talk about binary addition next lecture

Interpreting binary signed values

- Converting binary to signed: $B2T(X) = -x_{w-1} \cdot 2^{w-1} + \sum_{i=0}^{w-2} x_i \cdot 2^i$ $\sum_{i=0}^{w-1} \sum_{i=0}^{w-1} x_i \cdot 2^{i}$
- Note: most significant bit still tells us sign!! 1-> negative
 Checking if a number is negative is just checking that top bit
- Zero problem is solved too
 - 0b0000000 = 0 0b10000000 = -128
- -1: 0b111...1 = -1 (regardless of number of bits!)

Bounds of two's complement integers

- For a fixed width *w*, a limited range of integers can be expressed
 - Smallest value, most negative (we will call *TMin*):
 - 1 followed by all 0s bit pattern: $100...0 = -2^{w-1}$
 - Largest value, most positive (we will call *TMax*):
 - 0 followed by all 1s bit pattern: 01...1, value of $2^{w-1} 1$
- Beware the asymmetry! Bigger negative number than positive

Ranges for different bit amounts

	W			
	8	16	32	64
UMax	255	65,535	4,294,967,295	18,446,744,073,709,551,615
Umin	0	0	0	0
TMax	127	32,767	2,147,483,647	9,223,372,036,854,775,807
TMin	-128	-32,768	-2,147,483,648	-9,223,372,036,854,775,808

- Observations
 - |TMin| = TMax + 1
 - Asymmetric range
 - UMax = 2 * TMax + 1

- C Programming
 - #include <limits.h>
 - Declares constants, e.g.,
 - ULONG_MAX
 - LONG_MAX
 - LONG_MIN
 - Values are platform specific

Unsigned & Signed Numeric Values

X	B2U(<i>X</i>)	B2T(<i>X</i>)
0000	0	0
0001	1	1
0010	2	2
0011	3	3
0100	4	4
0101	5	5
0110	6	6
0111	7	7
1000	8	-8
1001	9	-7
1010	10	-6
1011	11	-5
1100	12	-4
1101	13	-3
1110	14	-2
1111	15	-1

• Equivalence

• Same encodings for non-negative values

Uniqueness

- Every bit pattern represents unique integer value
- Each representable integer has unique bit encoding

• \Rightarrow Can Invert Mappings

- Can go from bits to number and back, and vice versa
- $U2B(x) = B2U^{-1}(x)$
 - Bit pattern for unsigned integer
- $T2B(x) = B2T^{-1}(x)$
 - Bit pattern for two's complement integer

Practice + Break

- What range of integers can be represented with 5-bit two's complement?
 - A -31 to +31
 - B -15 to +15
 - C 0 to +31
 - D -16 to +15
 - E -32 to +31

Practice + Break

- What range of integers can be represented with 5-bit two's complement?
 - A -31 to +31
 B -15 to +15
 C 0 to +31
 D -16 to +15
 E -32 to +31
 No asymmetry and 6-bits
 No asymmetry
 No a

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Casting signed to unsigned

• C allows conversions from signed to unsigned (and vice versa)

short int	x = 15213;
unsigned short int	x = (unsigned short) x;
short int	y = -15213;
unsigned short int	<pre>uy = y; /* implicit cast! */</pre>

- Resulting value
 - Not based on current decimal value: instead keep the bits and *reinterpret* them!
 - Non-negative values unchanged
 - ux = 15213
 - Negative values change into (large) positive values (and vice versa)
 - *uy* = 50323
- Warning: Casts can be implicit in assignments or function calls!
 - More on that in a few slides

Mapping Signed \leftrightarrow Unsigned (4 bits)

Bits	Signed		Unsigned
0000	0		0
0001	1		1
0010	2		2
0011	3	. = .	3
0100	4		4
0101	5		5
0110	6		6
0111	7		7
1000	-8		8
1001	-7		9
1010	-6	+ 16 (i.e., 2 ⁴)	10
1011	-5		11
1100	-4	- 16 (i.e., 2 ⁴)	12
1101	-3		13
1110	-2		14
1111	-1		15

Large negative value becomes large positive!

Signed vs Unsigned in C

- Constants
 - By default constants are considered to be **signed integers**
 - Unsigned with "U/u" as suffix: 0U, 4294967259U
- Expression evaluation
 - If there is a mix of unsigned and signed in a single expression, signed values are converted to unsigned
 - Including comparison operations!! <, >, ==, <=, >=
- Can lead to surprising behavior!
 - $-1 < 0U \Rightarrow$ false!
 - -1 gets converted to unsigned
 - All 1s bit pattern \Rightarrow UMax! Definitely not less than 0!

• Convert signed 8-bit number -120 into an unsigned number

1. Convert -120 into binary

2. Convert binary back into unsigned decimal

• Convert signed 8-bit number -120 into an unsigned number

1. Convert -120 into binary -120 = -128 + 8 =

2. Convert binary back into unsigned decimal

• Convert signed 8-bit number -120 into an unsigned number

1. Convert -120 into binary -120 = -128 + 8 = 1x(-128) + 0x64 + 0x32 + 0x16 + 1x8 + 0x4 + 0x2 + 0x10b 1000 1000

2. Convert binary back into unsigned decimal

• Convert signed 8-bit number -120 into an unsigned number

1. Convert -120 into binary -120 = -128 + 8 = 1x(-128) + 0x64 + 0x32 + 0x16 + 1x8 + 0x4 + 0x2 + 0x1 $0b \ 1000 \ 1000$

2. Convert binary back into unsigned decimal 1x128 + 0x64 + 0x32 + 0x16 + 1x8 + 0x4 + 0x2 + 0x1128 + 8 = 136

Outline

- Binary and Hex
- Memory
- Encoding

Integer Encodings

- Signed Integers
- Converting Sign
- Converting Length
- Other encodings

Truncation

- May want to convert between numeric types of different sizes
- Going from a larger to a smaller number of bits is easy
 - **Truncation**: drop bits from the most significant side until we fit
 - Values that can be represented by both types are preserved!
 - Including negative values!
 - Values that can't be represented by the smaller type are mapped to some that can (modular (= modulo) behavior)
- Example
 - 16 bits \rightarrow 8 bits: 10110010 01001000 \rightarrow 01001000
 - Unsigned: $45640_{10} \rightarrow 72_{10}$ • $72_{10} = 45640_{10} \text{ modulo } 2^8$
 - Signed: $-52664_{10} \rightarrow 72_{10}$ • $72_{10} = -52664_{10}$ modulo 2^8

Extension

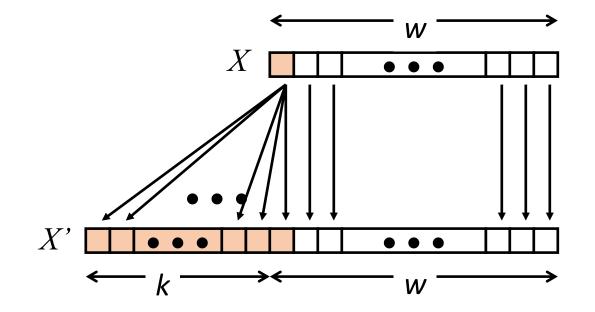
- Going from smaller to larger: what to do with the "new" bits?
 - These "new" bits go on the most significant side
- **Unsigned**: easy, pad with 0s!
 - Always safe to add 0s on the most significant end: $15213_{10} = 00015213_{10}$
 - Example: 8 bits \rightarrow 16 bits: 01001000 \rightarrow 0000000 01001000

•
$$72_{10} = 72_{10}$$

• Value is preserved!

Sign Extension

- Extending **signed** encodings takes more effort to preserve the value
- Duplicate the Most significant bit when extending
 - If it's a zero, extend with zeros. If it's a one, extend with ones.



Example sign extension

• Extend -128 from an 8-bit to bigger versions

- 8-bit version:
 - -128 + 0 = 1x(-128) + all zeros = 0b1000 0000
- 9-bit version:
 - -256 + 128 = 1x(-256) + 1x128 + all zeros = 0b1 1000 0000
- 10-bit version:
 - $-512 + 256 + 128 = 0b11\ 1000\ 0000$

Sign Extension Examples

```
signed short x = 15213;
signed int ix = (int) x;
signed short y = -15213;
signed int iy = (int) y;
```

	Decimal	Hex	Binary
x	15213	_3B_6D	00111011 01101101
ix	15213	00 00 3B 6D	0000000 0000000 00111011 01101101
У	-15213	C4 93	11000100 10010011
iy	-15213	FF FF C4 93	11111111 1111111 11000100 10010011

- Converting from smaller to larger integer data type
- C automatically performs sign extension for signed types
 - If cast changes both sign and size, extends based on *source* signedness
 - But less confusing to write code that makes the types (and casts) explicit

Break + Practice

• Convert 16-bit 0x3427 to an 8-bit signed integer

• Convert 8-bit 0xF0 to a 16-bit signed integer

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
Α	10	1010
В	11	1011
С	12	1100
D	13	1101
E	14	1110
F	15	1111

Break + Practice

- Convert 16-bit 0x3427 to an 8-bit signed integer
 - Process: truncate extra bits
 - Answer is **0x27**

• Convert 8-bit 0xF0 to a 16-bit signed integer

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
Α	10	1010
В	11	1011
С	12	1100
D	13	1101
E	14	1110
F	15	1111

Break + Practice

- Convert 16-bit 0x3427 to an 8-bit signed integer
 - Process: truncate extra bits
 - Answer is **0x27**

- Convert 8-bit 0xF0 to a 16-bit signed integer
 - Process: sign extend. Is the most-significant bit one? Yes!
 - Answer is **0xFFF0**

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
Α	10	1010
В	11	1011
С	12	1100
D	13	1101
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- Integer Encodings
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Encoding strings (The C way)

- Represented by array of characters
 - Each character encoded in ASCII format
 - NULL character (code 0) to mark the end
- Compatibility
 - Byte ordering not an issue (data all single-byte!)
 - ASCII text files generally platform independent
 - Except for different conventions of line termination character(s)!

Big-Endian Little-Endian

$$0x31 \longrightarrow 0x31$$

 $0x38 \longrightarrow 0x38$
 $0x32 \longrightarrow 0x32$
 $0x34 \longrightarrow 0x34$
 $0x33 \longrightarrow 0x33$
 $0x00 \longrightarrow 0x00$

Encoding color

- RGB colors
 - 3-byte values
 - First byte is Red, then Green, then Blue

- Usually specified in hexadecimal
 - #FF0000 -> maximum red, zero green or blue
 - #4E2A84 -> 1/4 red, 1/8 blue, 1/2 green (Northwestern Purple)
- 2^{24} possible colors = 16777216 colors

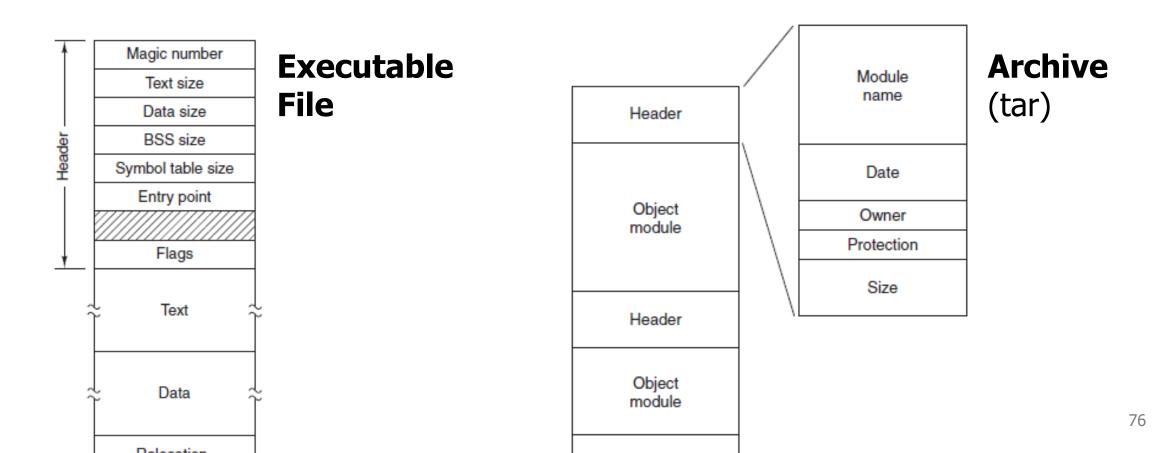
Interpreting file contents

- Collections of data
 - Usually in permanent storage on your computer

- Regular files
 - Arbitrary data
 - Think of as a big array of bytes
- Non-regular files would be directories, symbolic links, or other less used things

What about different types of regular files?

- Text files versus Executables versus Tar files
 - All just differing patterns of bytes!
 - It really is just all data. The meaning is in how you interpret it.



Identifying regular files

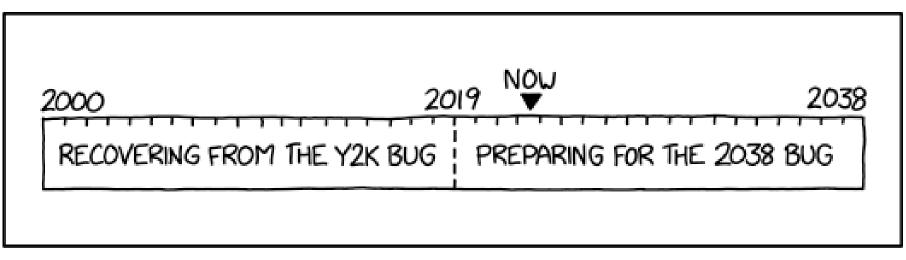
- file in Linux command line can help determine the type of a file
 - <u>https://github.com/file/file</u>

arguments arguments.c [brghena@ubuntu code] \$ file arguments.c arguments.c: C source, ASCII text [brghena@ubuntu code] \$ file arguments arguments: ELF 64-bit LSB shared object, x86-64, version 1 (SYSV), dynamically linked, interpreter /lib64 /ld-linux-x86-64.so.2, BuildID[sha1]=8731c4961d371f4989cd1b056f796ad54b711e6f, for GNU/Linux 3.2.0, not s tripped [brghena@ubuntu code] \$ file ./ ./: directory [brghena@ubuntu code] \$ file ~/scratch/GlobalProtect_UI_deb-5.1.0.0-101.deb /home/brghena/scratch/GlobalProtect_UI_deb-5.1.0.0-101.deb: Debian binary package (format 2.0), with cont rol.tar.gz, data compression xz

Encoding time

- Unix time:
 - 32-bit signed integer counting seconds elapsed since initial time
 - Initial time was January 1st at midnight UTC, 1970
- Current Unix time (as of last editing this slide): 1672850392
 - Negative numbers would mean times before 1970
- Problem: when does Unix time hit the maximum value?
 - 2147483647 seconds from January 1^{st} 1970
 - Result: January 19th, 2038
 - This is the "Year 2038 Problem"

Bonus xkcd comic



REMINDER: BY NOW YOU SHOULD HAVE FINISHED YOUR Y2K RECOVERY AND BE SEVERAL YEARS INTO 2038 PREPARATION.

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