Lecture 06 Arithmetic Instructions

CS213 – Intro to Computer Systems Branden Ghena – Spring 2021

Slides adapted from:

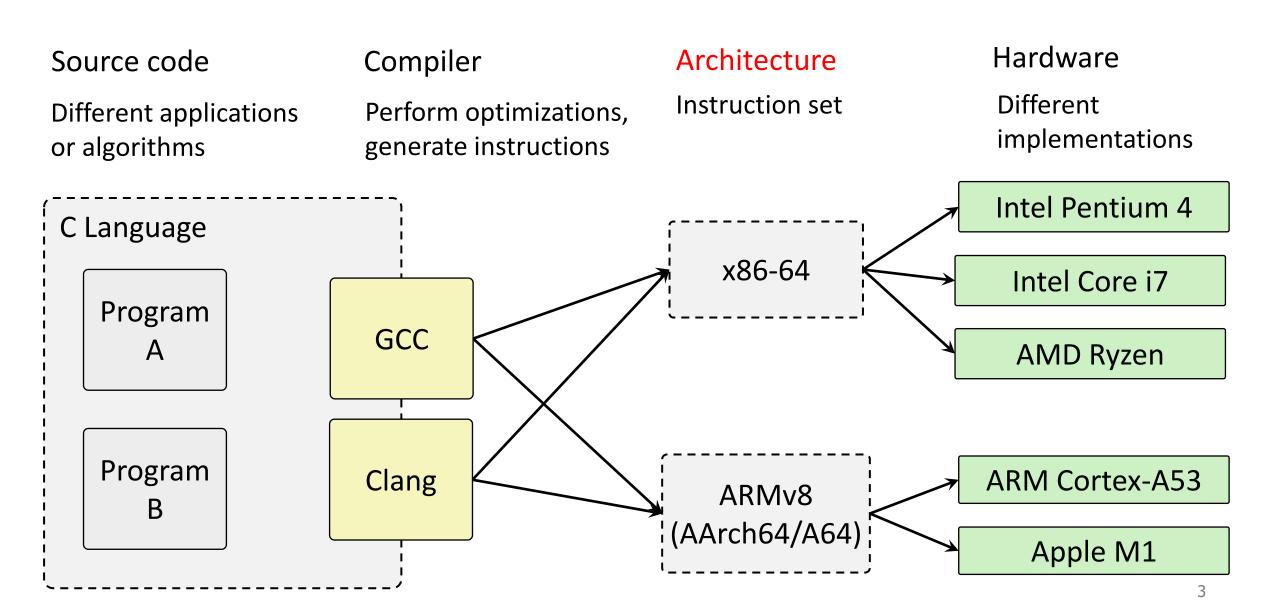
St-Amour, Hardavellas, Bustamente (Northwestern), Bryant, O'Hallaron (CMU), Garcia, Weaver (UC Berkeley)

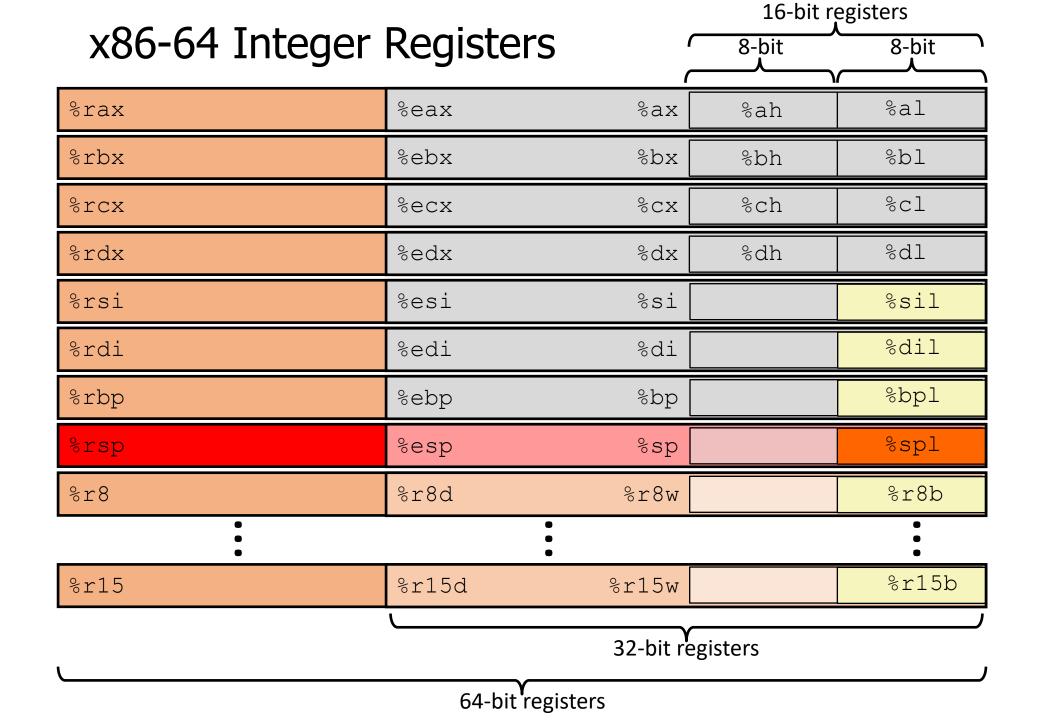
Administrivia

- Data Lab due tonight
 - 10% penalty per late day (or portion thereof)
- Homework 2 released. Bomb Lab released

- Exam next week Thursday (during class)
 - Details on this Thursday
 - There will be an alternate time for students abroad

Instruction Set Architecture sits at software/hardware interface





Operand Combinations



Cannot do memory-memory transfer with a single instruction

How would you do it? 1) Mem->Reg, 2) Reg->Mem

Three Basic Kinds of Instructions

- 1. Transfer data between memory and register
 - Load data from memory into register
 - %reg = Mem[address]
 - Store register data into memory
 - Mem[address] = %reg

Remember: Memory is indexed just like an array of bytes!

2. Perform arithmetic operation on register or memory data

•
$$c = a + b;$$
 $z = x << y;$ $i = h \& g;$

- 3. Control flow: what instruction to execute next
 - Unconditional jumps to/from procedures
 - Conditional branches

In x86-64 these basic types can often be combined

Today's Goals

- Continue exploring x86-64 assembly
 - Arithmetic
- Discuss real-world x86-64
 - Special cases
 - Generating assembly
- Understand condition codes
 - Method for testing Boolean conditions

Outline

Arithmetic Instructions

- Special Cases
 - Non 64-bit Data
 - Load Effective Address

Condition Codes

Viewing x86-64 Assembly

Some arithmetic operations

Two-operand instructions

Instruction	Effect	Description
addq S,D	D ← D + S	Add
subq S,D	D ← D − S	Substract
imulq S,D	D ← D * S	Multiply
xorq S,D	D ← D ^ S	Exclusive or
orq S,D	D ← D S	Or
andq S,D	D ← D & S	And

Operand types

- Immediate
- Register
- Memory (Only one can be memory)

Shifts

Instruction	Effect	Description
sarq k, D	D ← D >> k	Shift arithmetic right
shrq k, D	D ← D >> k	Shift logical right
salq k, D	D ← D << k	Shift left
shlq k, D	D ← D << k	Shift left (same as salq)

Be careful with operand order!!! (Matters for some operations)

A note on instruction names

- Instruction names can look somewhat arcane
 - shlq? movzbl?



rlwbv - Rotate Left Wheel and Buy a Vowel

5:06 PM - 20 Jan 2015

- But, good news: names (usually) follow conventions
 - Common prefixes (add), suffixes (b, w, 1, q), etc.
 - So you can understand pieces separately
 - Then combine their meanings

Some Arithmetic Operations

• Unary (one-operand) Instructions:

Instruction	Effect	Description
incq D	D ← D + 1	Increment
decq D	D ← D − 1	Decrement
negq D	D ← -D	Negate
notq D	D ← ~D	Complement

• See Section 3.5.5 for more instructions: mulq, cqto, idivq, divq

• Suppose a → %rax, b → %rbx, c → %rcx Convert the following C statement to x86-64:

$$a = b + c;$$

• Suppose a → %rax, b → %rbx, c → %rcx Convert the following C statement to x86-64:

$$a = b + c;$$

movq %rbx, %rax addq %rcx, %rax

• Suppose a → %rax, b → %rbx, c → %rcx Convert the following C statement to x86-64:

$$a = b + c;$$

```
movq $0, %rax addq %rbx, %rax addq %rcx, %rax
```

Is this okay?

• Suppose a → %rax, b → %rbx, c → %rcx Convert the following C statement to x86-64:

$$a = b + c;$$

```
movq $0, %rax addq %rbx, %rax addq %rcx, %rax
```

Is this okay?

Yes: just a little slower

• Suppose a → %rax, b → %rbx, c → %rcx Convert the following C statement to x86-64:

$$a = b + c;$$

```
addq %rbx, %rcx
movq %rcx, %rax
```

Is this okay?

• Suppose a → %rax, b → %rbx, c → %rcx Convert the following C statement to x86-64:

$$a = b + c;$$

addq %rbx, %rcx movq %rcx, %rax

Is this okay?

No: overwrites C

Question + Break

Reminder

addq, src, $dst \rightarrow dst = dst + src$

Suppose a → %rax, b → %rbx, c→ %rcx
 Convert the following C statement to x86-64:

$$c = (a-b) + 5;$$

```
[A] [B] movq %rax, %rcx movq %rax, %rcx subq %rbx, %rcx addq $5, %rcx movq $5, %rcx [C] subq %rcx, %rax, %rbx addq %rcx, %rcx, $5 addq $5, %rax movq %rax, %rcx
```

Question + Break

Reminder

addq, src, $dst \rightarrow dst = dst + src$

Suppose a → %rax, b → %rbx, c→ %rcx
 Convert the following C statement to x86-64:

$$c = (a-b) + 5;$$

```
movq %rax, %rcx
subq %rbx, %rcx
addq $5, %rcx

[C]
subq %rcx, %rax, %rbx
addq %rcx, %rcx, $5
Not x86
```

```
[B]
movq %rax, %rcx
subq %rbx, %rcx
movq $5, %rcx
```

c = 5

Overwrites a

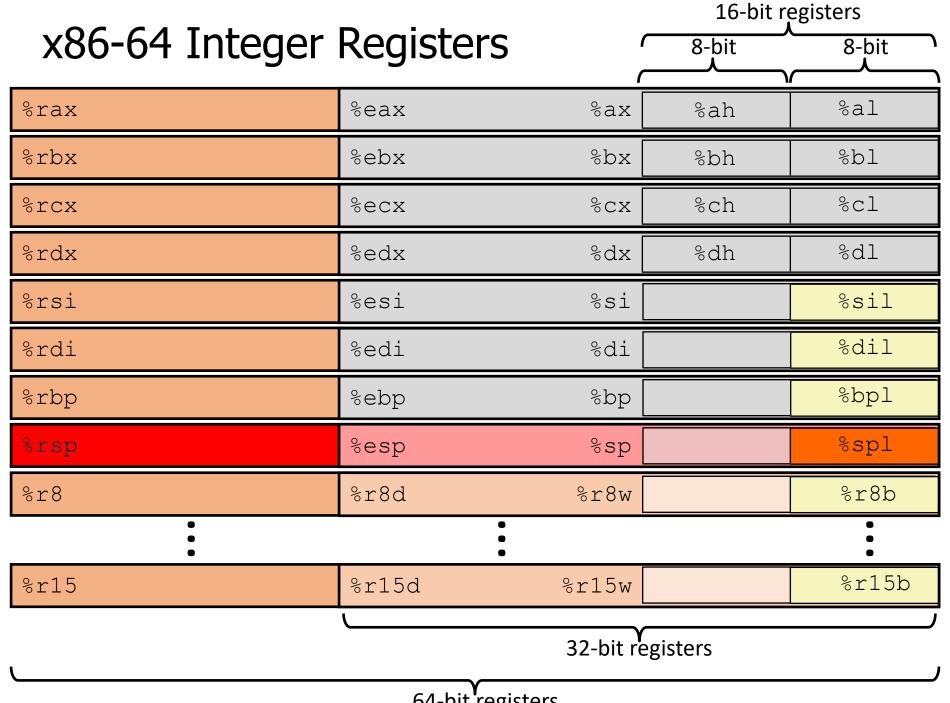
Outline

Arithmetic Instructions

- Special Cases
 - Non 64-bit Data
 - Load Effective Address

Condition Codes

Viewing x86-64 Assembly



Moving data of different sizes

- "Vanilla" move can only move between source and dest of the same size
 - Larger → smaller: use the smaller version of registers
 - Smaller → larger: extension! We have two options!

Instruction	Effect	Description
$movX S,D$ $X \in \{q, 1, w, b\}$	D ← S	Copy quad-word (8B), long- word (4B), word (2B) or byte (1B)
movsXX S,D XX∈{bw,bl,wl,bq,wq,lq}	D ← SignExtend(S)	Copy sign-extended byte to word, byte to long-word, etc.
movzXX S,D XX∈{bw,bl,wl,bq,wq,lq}	D ← ZeroExtend(S)	Copy zero-extended byte to word, byte to long-word, etc.
cltq	%rax ← SignExtend(%eax)	Sign-extend %eax to %rax

Example: moving byte data

• Note the differences between movb, movsbl and movzbl

• Assume %dl = 0xCD, %eax = 0x98765432

```
movb %dl,%al %eax = 0x987654CD movsbl %dl,%eax %eax = 0xFFFFFCD movzbl %dl,%eax %eax = 0x000000CD
```

32-bit Instruction Peculiarities

 Instructions that move or generate 32-bit values also set the upper 32 bits of the respective 64-bit register to zero, while 16 or 8 bit instructions don't.

• This includes 32-bit arithmetic! (e.g., addl)

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Complete Memory Addressing Modes

General:

```
D(Rb,Ri,S)
Rb: Base register (any register)
Ri: Index register (any register except %rsp)
S: Scale factor (1, 2, 4, 8) (sizes of common C types)
D: Constant displacement value (a.k.a. immediate)
```

```
• Mem[ Reg[Rb] + Reg[Ri]*S + D ]
```

Saving computed addresses

- Generally, any instruction with () in it, accesses memory
 - Address is computed first
 - Load if in a source operand
 - Store if in a destination operand
- But what if what you really want is the address?
 - lea load effective address
 - Exception to () rule. Does NOT load from memory
 - Also generally useful for arithmetic

Address computation instruction

• leaq src, dst

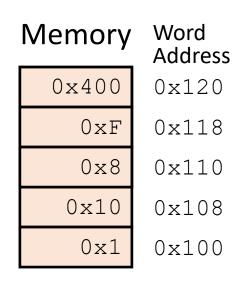
- "lea" stands for *load effective address*
- src is address expression (any of the formats we've seen)
- dst is a register
- Sets dst to the address computed by the src expression (does not go to memory! it just does math)
- Example: leaq (%rdx,%rcx,4), %rax

• Uses:

- Computing addresses without a memory reference
 - *e.g.* translation of p = &x[i];
- Computing arithmetic expressions of the form x+k*i+d
 - Though k can only be 1, 2, 4, or 8

Example: lea vs. mov

Registers %rax %rbx %rcx 0x4 %rdx 0x100 %rdi %rsi



```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```

Example: lea vs. mov

Registers

%rax	0x110
%rbx	0 x 8
%rcx	0×4
%rdx	0x100
%rdi	
%rsi	

Memory Word Address

0x400	0x120
0xF	0x118
0x8	0x110
0x10	0x108
0x1	0x100

```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```

Example: lea vs. mov

Registers %rax 0x110

%rbx	0 x 8

0x4

%rdx	0x100
------	-------

Memory Word Address

0x400	0x120
0xF	0x118
0x8	0x110
0x10	0x108
0x1	0x100

```
leaq (%rdx,%rcx,4), %rax
movq (%rdx,%rcx,4), %rbx
leaq (%rdx), %rdi
movq (%rdx), %rsi
```

```
int arith (long x, long y, long z) {
  long t1 = x+y;
  long t2 = z+t1;
  long t3 = x+4;
  long t4 = y * 48;
  long t5 = t3 + t4;
  long rval = t2 * t5;
  ....
}
```

```
leaq (%rsi,%rdi),%rcx
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- Don't expect a 1-1 mapping

```
# rdi = x
# rsi = y
# rdx = z
# rcx = x+y (t1)
```

```
int arith (long x, long y, long z) {
  long t1 = x+y;
  long t2 = z+t1;
  long t3 = x+4;
  long t4 = y * 48;
  long t5 = t3 + t4;
  long rval = t2 * t5;
  ....
}
```

```
leaq (%rsi,%rdi),%rcx
leaq (%rsi,%rsi,2),%rsi
salq $4,%rsi
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- Don't expect a 1-1 mapping

```
# rdi = x
# rsi = y
# rdx = z
# rcx = x+y (t1)
# rsi = y + 2*y = 3*y
# rsi = (3*y)*16 = 48*y (t4)
```

```
int arith (long x, long y, long z) {
  long t1 = x+y;
  long t2 = z+t1;
  long t3 = x+4;
  long t4 = y * 48;
  long t5 = t3 + t4;
  long rval = t2 * t5;
  ....
}
```

```
leaq (%rsi,%rdi),%rcx
leaq (%rsi,%rsi,2),%rsi
salq $4,%rsi
addq %rdx,%rcx
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- Don't expect a 1-1 mapping

```
# rdi = x
# rsi = y
# rdx = z
# rcx = x+y (t1)
# rsi = y + 2*y = 3*y
# rsi = (3*y)*16 = 48*y (t4)
# rcx = z+t1 (t2)
```

```
int arith (long x, long y, long z) {
  long t1 = x+y;
  long t2 = z+t1;
  long t3 = x+4;
  long t4 = y * 48;
  long t5 = t3 + t4;
  long rval = t2 * t5;
  ....
}
```

```
leaq (%rsi,%rdi),%rcx
leaq (%rsi,%rsi,2),%rsi
salq $4,%rsi
addq %rdx,%rcx
leaq 4(%rsi,%rdi),%rdi
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- Don't expect a 1-1 mapping

```
# rdi = x
# rsi = y
# rdx = z
# rcx = x+y (t1)
# rsi = y + 2*y = 3*y
# rsi = (3*y)*16 = 48*y (t4)
# rcx = z+t1 (t2)
# rdi = t4+x+4 (t5)
```

```
int arith (long x, long y, long z) {
  long t1 = x+y;
  long t2 = z+t1;
  long t3 = x+4;
  long t4 = y * 48;
  long t5 = t3 + t4;
  long rval = t2 * t5;
  ....
}
```

```
leaq (%rsi,%rdi),%rcx
leaq (%rsi,%rsi,2),%rsi
salq $4,%rsi
addq %rdx,%rcx
leaq 4(%rsi,%rdi),%rdi
imulq %rcx,%rdi
```

- Compiler can reorder operations
- Can have one statement take multiple instructions
- Can have one instruction handle multiple statements
- Don't expect a 1-1 mapping

```
# rdi = x
# rsi = y
# rdx = z
# rcx = x+y (t1)
# rsi = y + 2*y = 3*y
# rsi = (3*y)*16 = 48*y (t4)
# rcx = z+t1 (t2)
# rdi = t4+x+4 (t5)
# rdi = t2*t5 (rval)
```

Outline

Arithmetic Instructions

- Special Cases
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Condition Codes

Viewing x86-64 Assembly

What can instructions do?

- Move data: √
- Arithmetic: ✓
- Transfer control: X
 - Instead of executing next instruction, go somewhere else
- Let's back out. Why do we want that?

```
if (x > y)
    result = x-y;
else
    result = y-x;
```

```
while (x > y)
    result = x-y;
return result;
```

- Sometimes we want to go from the red code to the green code
- But the blue code is what's next!
- Need to transfer control! Execute an instruction that is not the next one
- And conditionally, too! (i.e., based on a condition)

Condition codes

- Control is mediated via Condition codes
 - single-bit registers that record answers to questions about values
 - E.g., Is value x greater than value y? Are they equal? Is their sum even?
 - Let's keep "question" abstract for now. We'll see the details in a bit.
 - Terminology:
 - a bit is *set* if it is 1
 - a bit is *cleared* (or *reset*) if it is 0

Conditionals at the machine level

- At machine level, conditional operations are a 2-step process:
 - Perform an operation that sets or clears condition codes (ask questions)
 - Then observe which condition codes are set, do the operation (or not)
- Can express Boolean operations, conditionals, loops, etc.
 - We will see the first today, and more control next lecture
- So now we need three things:
 - 1. Instructions that compare values and set condition codes
 - 2. Instructions that observe condition codes and do something (or not)
 - 3. A set of actual condition codes (what questions do we track answers to?)

Two-Step Conditional Process: Bool Ops

- Lots of new pieces
- Lets give an example first, then learn more about each
 - Translate C code on right into assembly

```
char gt (int x, int y)
{
  return x > y;
}
```

Register	Use(s)	
%rdi	Argument x	
%rsi	Argument y	
%rax	Return value	

```
cmpq %rsi, %rdi # Compare x:y
setg %al # Set when x > y (i.e., %rdi > %rsi)
ret
```

Two-Step Conditional Process: Bool Ops

- Step 1, cmpq: compare quad words
 - compare the values in %rsi and %rdi, keep track of all you can learn, and set the relevant condition codes
 - Are the two equal? Set the condition codes that records they were equal
 - Was the right one greater?
 - Etc. We don't know yet which answer we are going to need!

```
char gt (int x, int y)
{
  return x > y;
}
```

Register	Use(s)	
%rdi	Argument x	
%rsi	Argument y	
%rax	Return value	

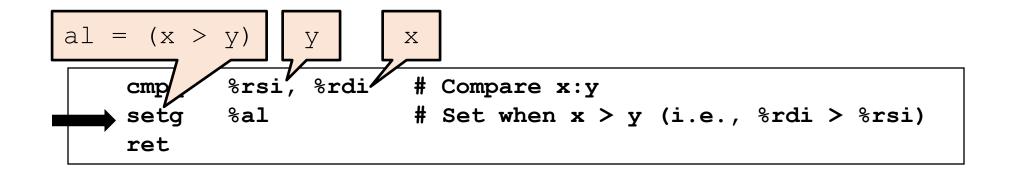
```
cmpq %rsi, %rdi # Compare x:y
setg %al # Set when x > y (i.e., %rdi > %rsi)
ret
```

Two-Step Conditional Process: Bool Ops

- Step 2, setX: set destination register to 1 if condition is met
 - setg = set if the 2nd operand is *greater* than the 1st (careful about the order!)
 - There's also set1 for less than, etc.
 - Reads the condition codes that encodes the answer to that question
 - Set the 1-byte register %al to 1 if true

```
char gt (int x, int y)
{
  return x > y;
}
```

Register	Use(s)	
%rdi	Argument x	
%rsi	Argument y	
%rax	Return value	



Step 1: Setting condition codes

- Analogy: Asking ALL the possible questions at once
 - And recording the answers
 - We don't know yet which question is the one we care about!
- Done in one of two ways
 - Implicitly: all* arithmetic instructions set (and reset) condition codes in addition to producing a result
 - * except lea; it's not "officially" an arithmetic instruction
 - **Explicitly**: by instructions whose sole purpose is to set condition codes
 - E.g., cmpq
 - They don't actually produce results (in registers or memory)
 - Condition codes are left unchanged by other operations

Implicitly Setting Condition Codes

- Condition codes on x86
 - **CF** Carry Flag (for unsigned) **SF** Sign Flag (for signed)
 - **ZF** Zero Flag **OF** Overflow Flag (for signed)
 - PF Parity Flag
 - Not an arbitrary set! By combining them, can keep track of answers to many useful questions! (We'll see exactly which in a bit.)

Implicitly Setting Condition Codes

```
CF (Carry) SF (Sign) ZF (Zero) OF (Overflow) PF (Parity)
```

- Set (or reset) based on the result of arithmetic operations
 Example: addq Src, Dest # C-analog: t = a+b
 - **ZF** set if t == 0
 - SF set if t < 0 (as signed)
 - CF set if carry out from most significant bit (unsigned overflow)
 also CF takes the value of the last bit shifted (left or right)
 - OF set if twos-complement (signed) overflow (pos/neg overflow)
 (a>0 && b>0 && t<0) || (a<0 && b<0 && t>=0)
 also, set if a 1-bit shift operation changes the sign of the result
 - **PF set** if t has an even number of 1 bits

Explicitly Setting Condition Codes: Compare

- cmp{b,w,l,q} Src2, Src1
- cmpq b, a computes t = a-b, then throws away the result!
 - And sets condition codes along the way, like subq would!
 - Follows the rules we saw on the previous slide for arithmetic instructions!
 - Beware the order of the cmp operands!
- More directly
 - **ZF** set if a == b
 - SF set if (a-b) < 0 (as signed), i.e., b > a in a signed comparison!
 - CF and OF used mostly in combinations with others (see in a few slides)

Explicitly Setting Condition Codes: Test

- test{b,w,l,q} *Src2,Src1*
- testq b, a computes t = a&b, then throws away the result!
 - And sets condition codes like andq would (order doesn't matter here)
 - So again, same rules as arithmetic instructions
- More directly
 - ZF set when a&b == 0, i.e., a and b have no bits in common
 - SF set when a&b < 0
- Useful when doing bit masking
 - E.g., x & 0x1, to know whether x is even or odd
 - If the result of the & is 0, it's even, if 1, it's odd

Step 2: Reading Condition Codes

- Cannot read condition codes directly; instead observe via instructions
 - And generally observe combinations of condition codes, not individual ones

- Example: the setx family of instructions
 - Write single-byte destination register based on combinations of condition codes
 - set{e, ne, s, ...} D where D is a 1-byte register
 - Example: sete %al
 - means: %al=1 if flag ZF is set, %al=0 otherwise

Condition codes combinations

SetX	Description	Condition
sete	Equal / Zero	ZF
setne	Not Equal / Not Zero	~ZF
sets	Negative	SF
setns	Nonnegative	~SF
setg	Greater (Signed)	~(SF^OF) &~ZF
setge	Greater or Equal (Signed)	~(SF^OF)
setl	Less (Signed)	(SF^OF)
setle	Less or Equal (Signed)	(SF^OF) ZF
seta	Above (unsigned)	~CF&~ZF
setb	Below (unsigned)	CF

Note: suffixes do not indicate operand sizes, but rather conditions

These same suffixes will come back when we see other instructions that read condition codes.

Step 2: Reading Condition Codes

- setx (and others) read the current state of condition codes
 - Whatever it is, and whichever instruction changed it last
- So when you see (for example) setne, work backwards!
 - Look at previous instructions, to find the last one to change conditions
 - Then you'll know the two values that were compared
 - Ignore instructions that don't touch condition codes (like moves)
- Usually you'll see a cmpx (or testx, or arithmetic) right before
 - But not always, so know what to do in general

Question + Break

• %rax = 15, %rbx = 15

cmpq %rax, %rbx

Which flag(s) are set?

CF (Carry) **SF** (Sign) **ZF** (Zero) **OF** (Overflow) **PF** (Parity)

Question + Break

• %rax = 15, %rbx = 15

• Which flag(s) are set?

```
CF (Carry) SF (Sign) ZF (Zero) OF (Overflow) PF (Parity)
```

- **ZF is set** (because the two are equal and subtracted)
- **PF is set** (because there are an even number of 1 bits, four total)

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Viewing x86-64 Assembly

How to Get Your Hands on Assembly

- From C source code, using a compiler
 - gcc -01 -s sum.c
 - Produces file sum.s
 - Online compiler, shows asm output: https://godbolt.org
 - *Warning*: May get very different results on different machines due to different versions of gcc and different compiler settings

C Code: sum.c

Generated x86-64 assembly: sum.s

```
sum:
   pushq %rbx
   movq %rdx, %rbx
   call plus
   movq %rax, (%rbx)
   popq %rbx
   ret
```

How to Get Your Hands on Assembly

- From machine code, using a disassembler
 - objdump -d sum.o
 - Within the gdb Debugger
 linux> gdb prog
 (gdb) disassemble sum
 - gdb tutorial coming soon!
 - *Warning*: Disassemblers are approximate; some information is lost during translation from assembly to machine code
 - Label names are lost, what is just data (vs code) is lost, etc.
 - Useful if you don't have the source

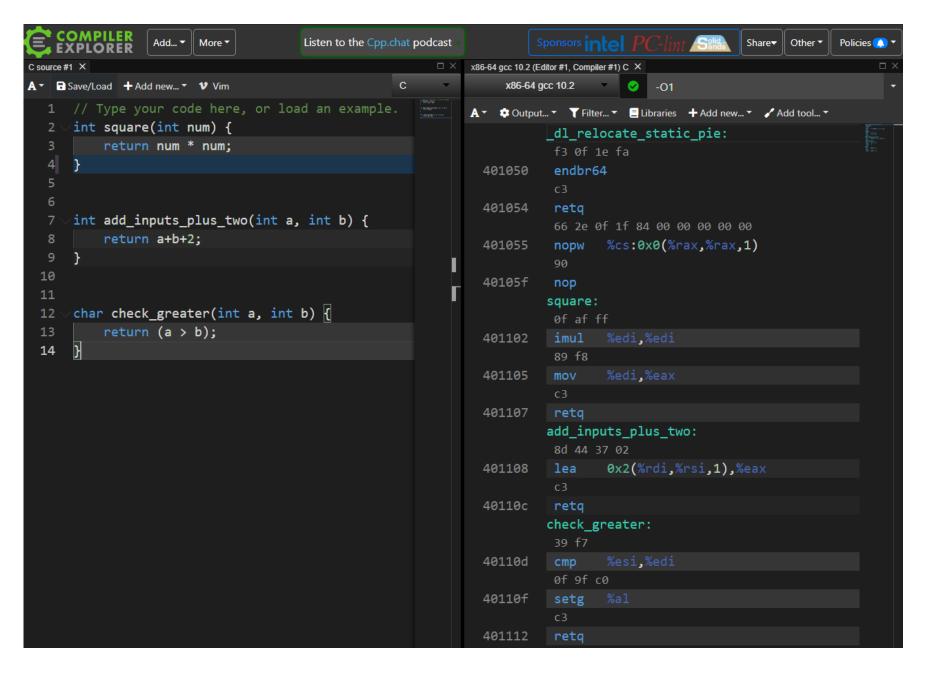
• Godbolt example!

Godbolt

Ignore "_dl_relocate_static_pie"

Play around with this to try stuff on your own

https://godbolt.org/



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