Lecture 12 Cache Memories

CS213 – Intro to Computer Systems Branden Ghena – Fall 2023

Slides adapted from:

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Today's Goals

- Discuss organization of various cache designs
 - Direct-mapped caches
 - N-way set-associative caches
 - Fully-associative caches

 Understand how cache memories are used to reduce the average time to access memory

Outline

Locality of Reference

Cache Organization

Associativity

Cache Performance

Caching speeds up code

- Cache: smaller, faster storage device that keeps copies of a subset of the data in a larger, slower device
 - If the data we access is already in the cache, we win!
 - Can get access time of faster memory, with overall capacity of larger

- But how do we decide which data to keep in the cache?
 - Can we predict which data is likely to be necessary in the future?

Locality

- Goal: predict which data the CPU will want to access
 - So we can bring it to (and keep it in!) fast memory
 - Problem: memory is huge! (billions of bytes) how do you decide which to save?
- Principle of Locality
 - Programs tend to reuse/use data items recently used or nearby those recently used
- Temporal locality
 - Recently referenced items are likely to be referenced in the near future
- Spatial locality
 - Items with nearby addresses tend to be referenced close together in time

Types of locality practice

- Temporal locality
 - Recently referenced items are likely to be referenced in the near future
- Spatial locality
 - Items with nearby addresses tend to be referenced close together in time

- Quiz: what kind of locality?
 - Data
 - Reference array elements in succession: Spatial locality
 - Reference sum each iteration: Temporal locality
 - Instructions
 - Execute instructions in sequence: Spatial locality
 - Cycle through loop repeatedly: Temporal locality

```
sum = 0;
for (i = 0; i < n; i++)
    sum += a[i];
return sum;</pre>
```

Locality example

- Can get a sense for whether a function has good locality just by looking at its memory access patterns
- Does this function have good locality?

```
int sumarrayrows(int a[M][N]) {
  int sum = 0;
  for (int i = 0; i < M; i++) {
    for (int j = 0; j < N; j++) {
       sum += a[i][j];
    }
  }
  return sum;
}</pre>
```

Temporal or spatial locality?

Spatial: accesses to array Temporal: accesses to sum

Yes!

- Array is accessed in same row-major order in which it is stored in memory
- a through a+3, a+4 through a+7, a+8 through a+11, etc.

Locality example

Does this function have good locality?

```
int sumarraycols(int a[M][N]) {
  int sum = 0;
  for (int j = 0; j < N; j++) {
    for (int i = 0; i < M; i++) {
       sum += a[i][j];
    }
  }
  return sum;
}</pre>
```

- · No!
 - Scans array column-wise instead of row-wise
 - a through a+3, then a+4*N through a+4*N+3, etc.
 - Holy jumping around memory Batman!
- More on that in a later lectures

Locality to the Rescue!

- How can we exploit locality to bridge the CPU-memory gap?
 - Use it to determine which data to put in a cache!
- Spatial locality
 - When level k needs a byte from level k+1, don't just bring one byte
 - Bring neighboring bytes as well!
 - Good chances we'll need them too in the near future
- Temporal locality
 - When you bring something into the cache, try to keep it there
 - Good chances we'll need it again in the near future
- Result: most accesses should be cache hits!
 - Memory system: size of largest memory, with speed close to that of fastest memory

Outline

Locality of Reference

Cache Organization

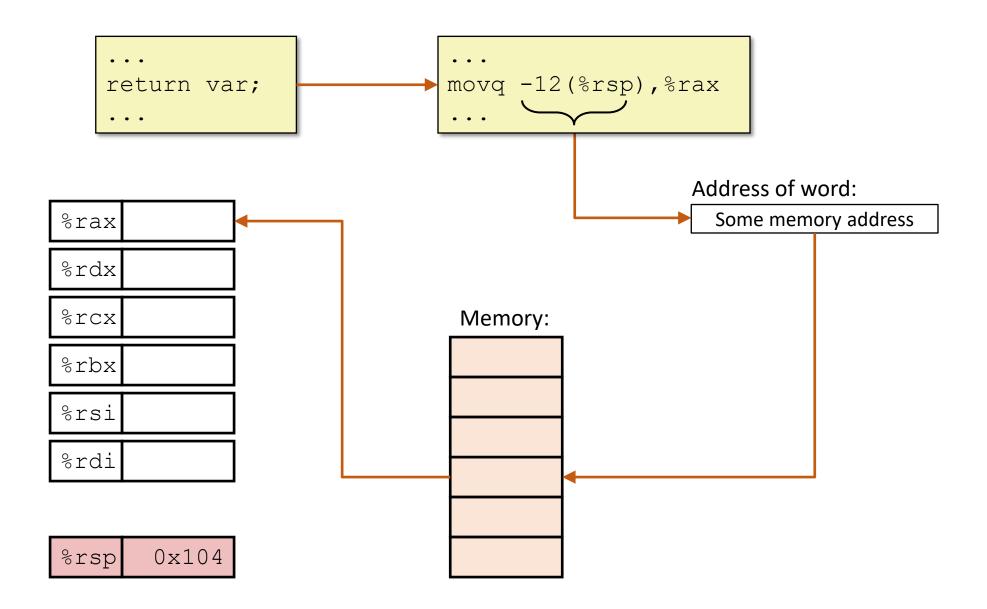
Associativity

Cache Performance

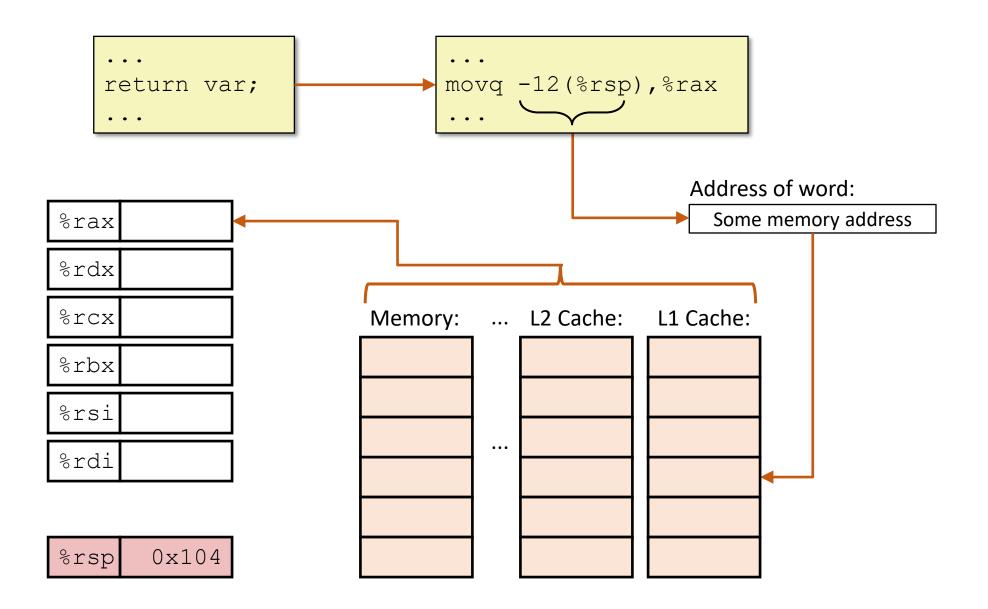
Cache memories

- A specific instance of the general principle of caching
 - Small, fast SRAM-based memories between CPU and main memory
 - Can include multiple levels
 - L1 = small, but really fast, L2 = larger, slower, L3, etc.
- CPU looks for data in caches first
 - e.g., L1, then L2, then L3, then finally in main memory as a last resort
- Mechanisms we'll see today are implemented in hardware

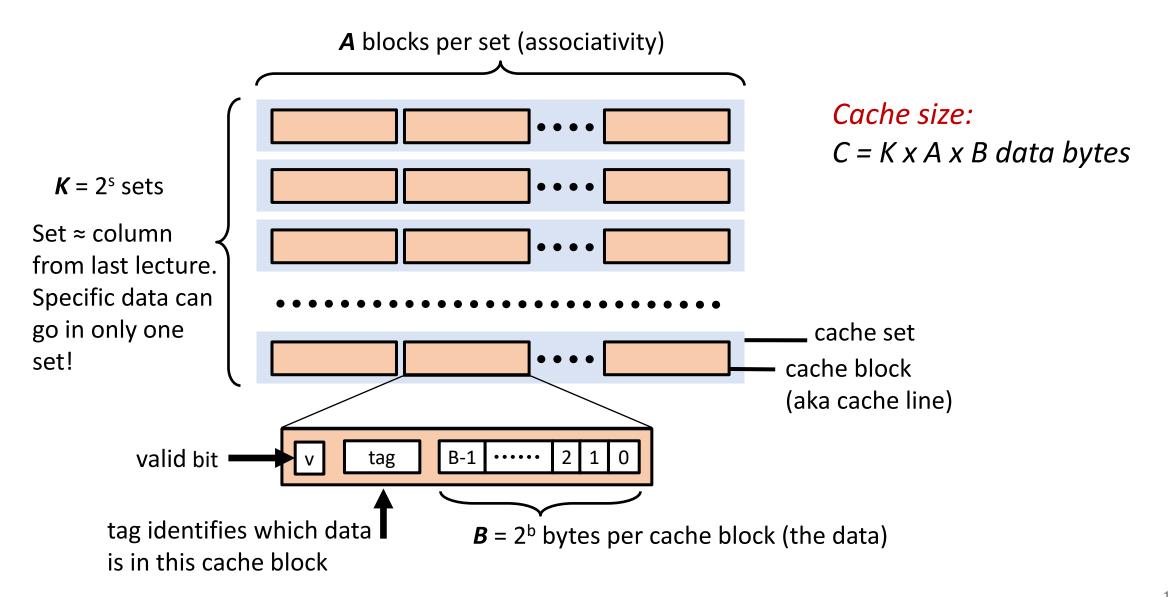
How You Probably Thought a Memory Access Worked



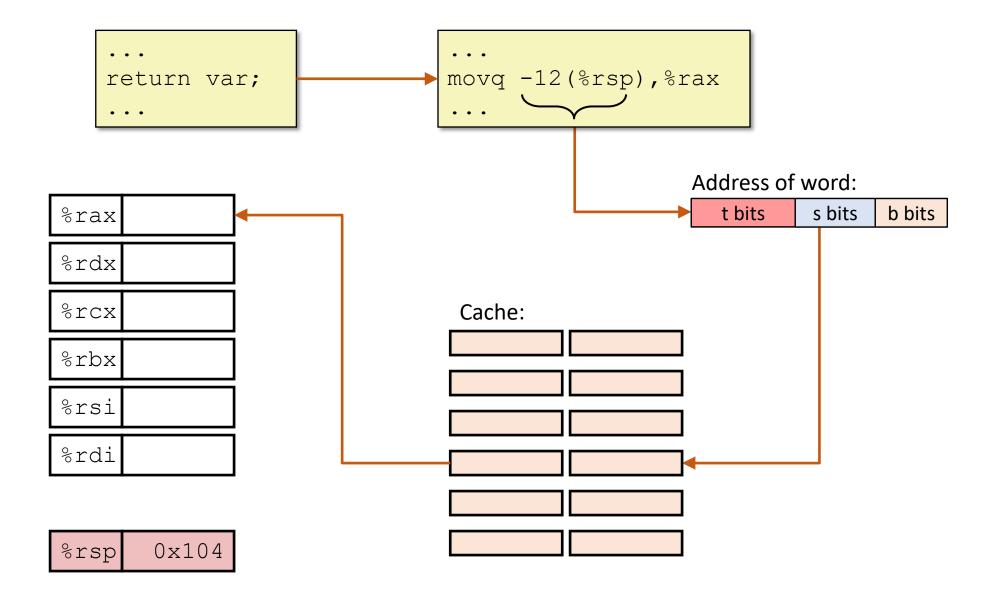
How a Memory Access Actually Works



General Cache Organization (S, A, B)

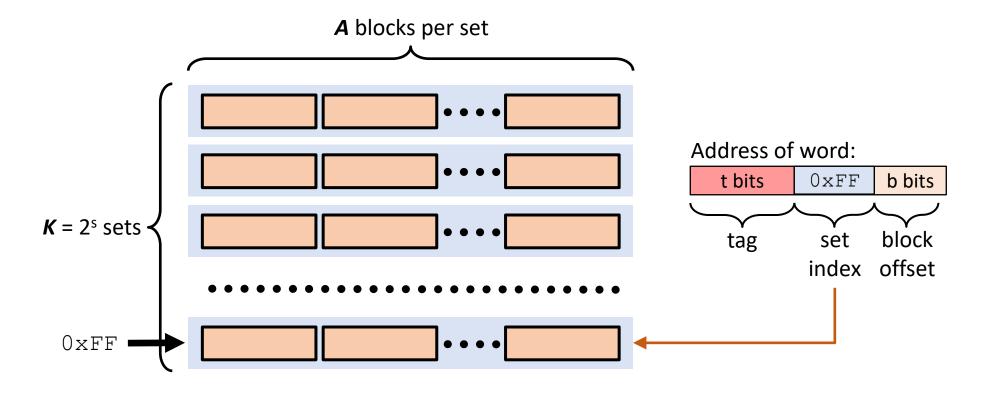


Cache Access



Cache Read (1): Locate Set

Locate set



Each address maps to a particular set!

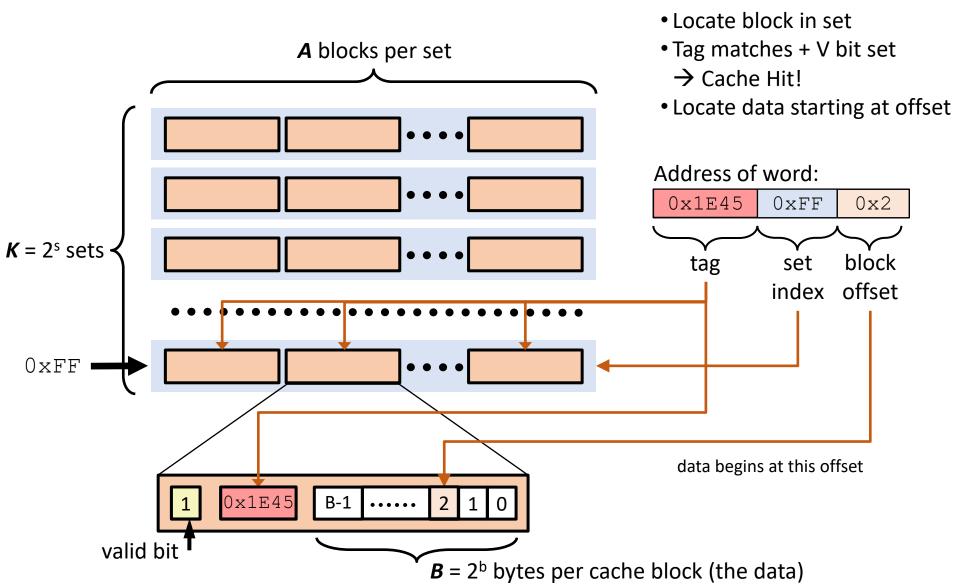
Data has to be stored at that particular set!

Even if that set is full and there "is space" elsewhere!

(That's where conflict misses come from.)

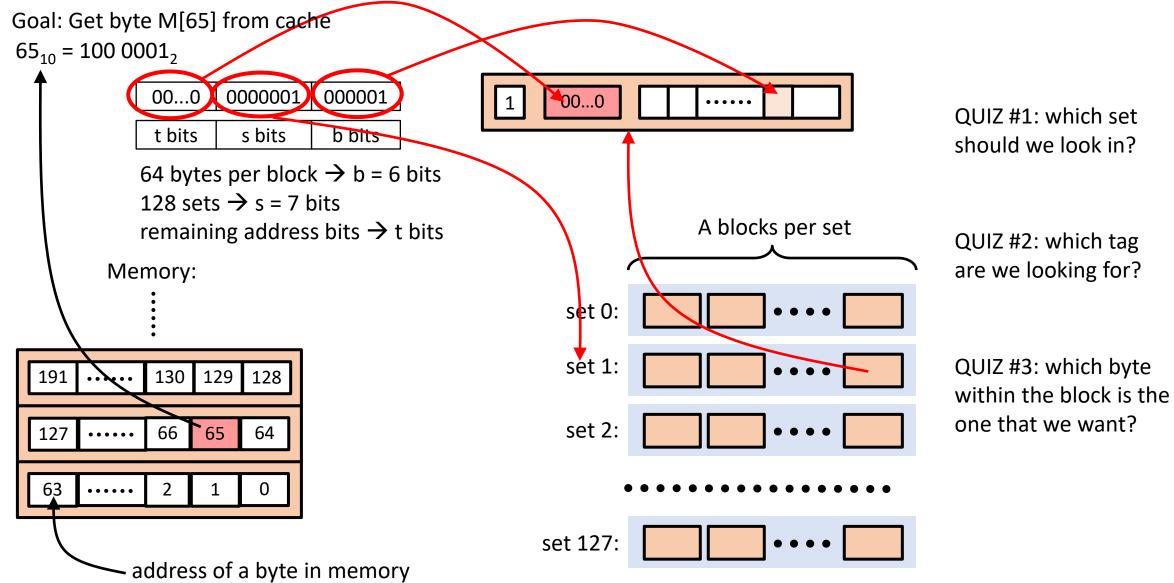
Cache Read (2): Tag Match + Valid Locate set Locate block in set • Tag matches + valid bit set **A** blocks per set → Cache Hit! Address of word: 0x1E45 0xFF b bits $K = 2^{s}$ sets block tag set index offset 0xFF Within a set, could be anywhere! So, need to check all blocks! 0x1E45 But if it's not in that set, it's not in the cache at all! (It's the only place it could be.) valid bit

Cache Read (3): Block Offset

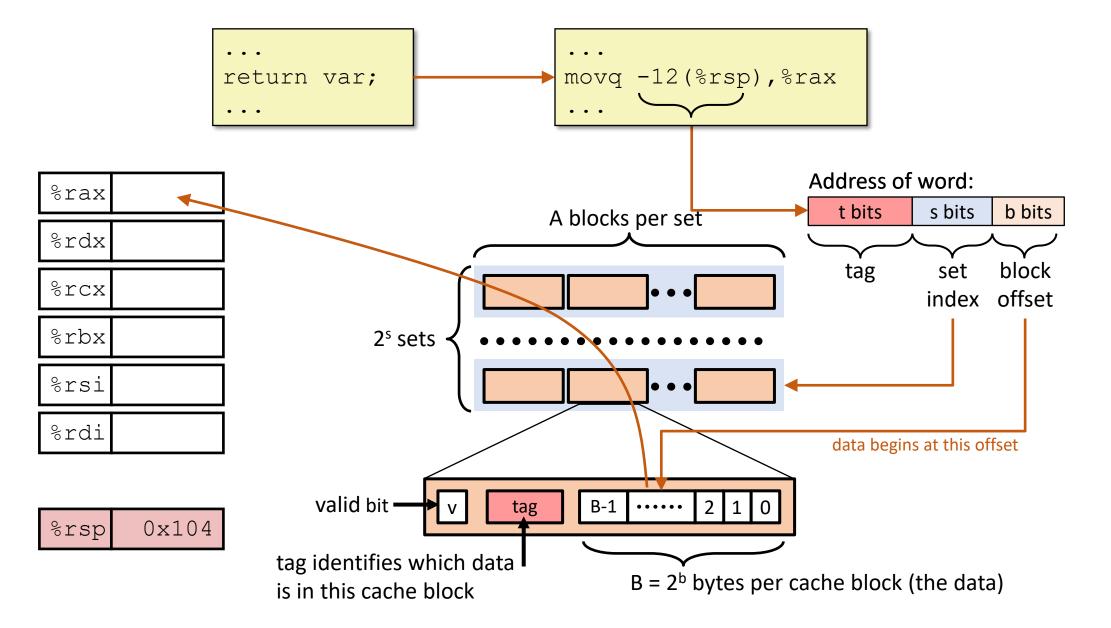


Locate set

Example: 128 sets, 64 bytes per block



Cache access overview



What about writes?

- Multiple copies of data exist:
 - L1, L2, Main Memory, Disk
 - Don't want them to get (or at least not to stay) out of sync!
 - Otherwise, who do you believe?

Multiple configuration options that a cache could have

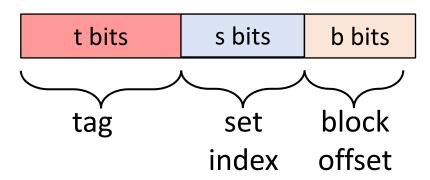
Write configurations

- What to do on a write-hit?
 - *Write-through* (write immediately to memory)
 - Write-back (delay write until we evict this cache block)
 - Need a dirty bit (indicate if block differs from memory)
 - We had an example of that last time
- What to do on a write-miss?
 - Write-allocate (load into cache, update block in cache)
 - Good if more writes to the location follow
 - No-write-allocate (writes immediately to memory, doesn't bring into cache)
- Typical combinations
 - Write-back + Write-allocate ← by far the most common
 - Write-through + No-write-allocate

Break + Question

- 64-bit, byte-addressed system
- 32 kB cache
 - 512 sets and 64-byte blocks
- How many bits for Tag?
 - A: 6 bits
 - B: 9 bits
 - C: 17 bits
 - D: 49 bits

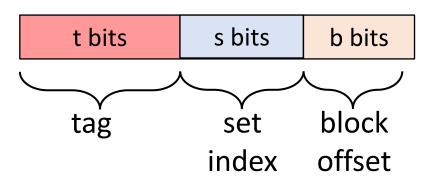
Address of word:



Break + Question

- 64-bit, byte-addressed system
- 32 kB cache
 - 512 sets and 64-byte blocks

Address of word:



- How many bits for Tag? (6 bits for block, 9 bits for set)
 - A: 6 bits
 - B: 9 bits
 - C: 17 bits
 - **D: 49 bits** (Tag is remaining bits. 64 6 9 = 49)

Outline

Locality of Reference

Cache Organization

Associativity

Cache Performance

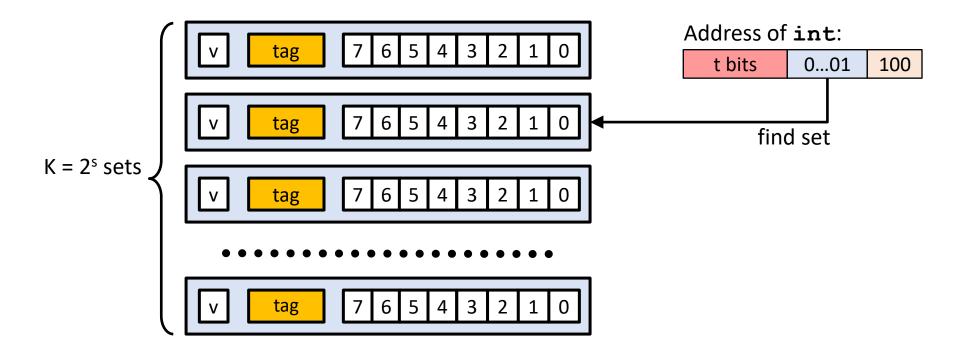
Cache memory associativity

- When designing a cache, a number of parameters to choose
 - Total size (C), cache block size (B), number of sets (K), ...
- The most interesting one: associativity (A)
 - i.e., how many cache blocks per set
 - Has a significant impact on effectiveness (and complexity!)

Associativity choices

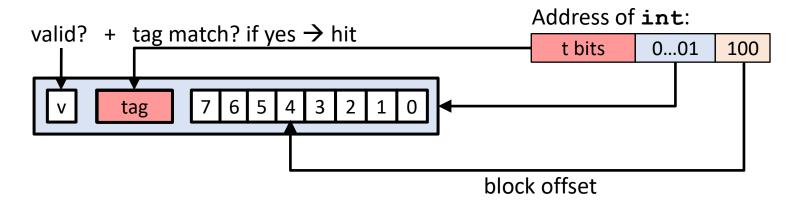
- Associativity 1 → direct-mapped caches
 - One cache block per set, data blocks can only go in that one cache block
 - Whenever we place data in a set, must evict whatever is there
- Associativity $>1 \rightarrow$ **set-associative caches**
 - Can keep multiple blocks that would map to the same set
- Single set → fully-associative caches
 - Any block can go anywhere, 1 big set, tag is all that matters
 - Very rare for cache memories due to expensive hardware

Direct mapped: One block per set Assume: cache block size 8 bytes



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Direct mapped: One block per set Assume: cache block size 8 bytes

valid? + tag match? if yes → hit

t bits

valid? + tag match? if yes → hit

t bits

valid? + tag match? if yes → hit

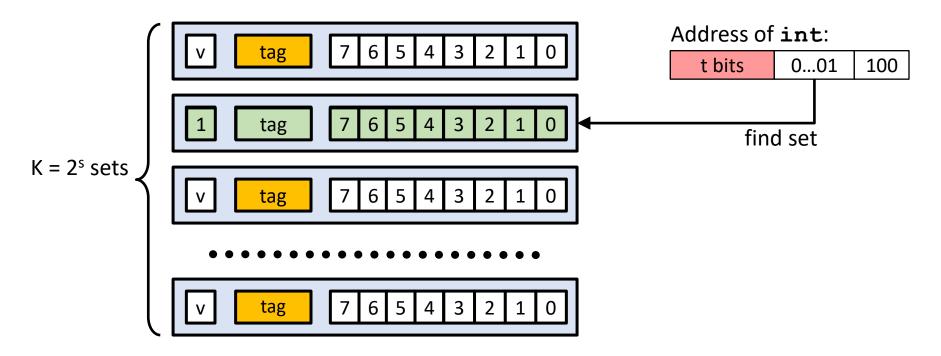
t bits

block offset

int is here (4 bytes)

Direct mapped: One block per set

Assume: cache block size 8 bytes



If tag doesn't match or valid bit is not set: cache miss!

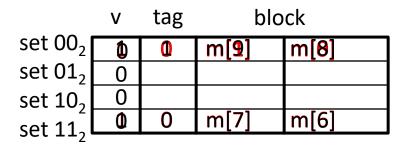
→ old block is evicted and replaced with currently requested one

Direct-mapped cache simulation

t=1	s=2	b=1
Х	XX	Х

Address trace (reads, one byte per read): $0 [0 00 0_2]$ miss

P154.5



M=16 addresses, byte-addressable

B=2 bytes/block

K=4 sets

A=1 blocks/set

7 [0 **11** 1₂] miss

1 [0 00 1₂]

 $8 [1 00 0_2]$ miss

 $0 [0 00 0_2]$ miss

What are the types of each miss here?

t=1	s=2	b=1
Х	XX	Х

M=16 addresses, byte-addressable B=2 bytes/block

K=4 sets

A=1 blocks/set

Address trace (reads, one byte per read): $0 [0 00 0_2]$ miss Compulsory

Miss

 $1[0 \ 00 \ 1_2]$ hit

7 [0 11 1₂] miss Compulsory Miss

8 [1 00 0₂] miss Compulsory

0 [0 00 0₂] miss Conflict

	V	tag	block	
set 00 ₂	1	0	m[1]	m[0]
set 01 ₂	0			
set 10 ₂	0			
set 11 ₂	1	0	m[7]	m[6]

Options:

- Compulsory
- Capacity
- Conflict

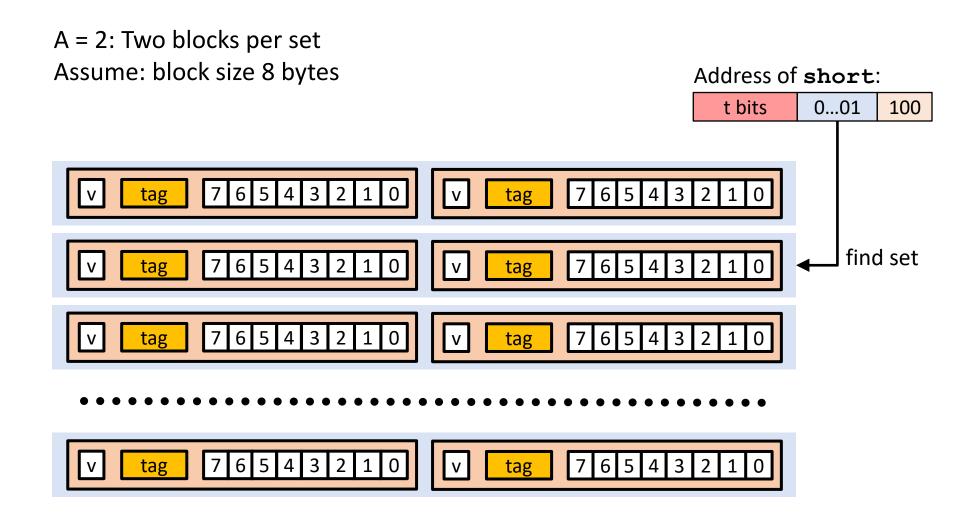
Conflict misses:

There is "room" in the cache, but two blocks map to the same set; one evicts the other! Pause for questions on direct-mapped caches

Associativity choices

- Associativity 1 → direct-mapped caches
 - One cache block per set, blocks can only go in that one block
 - Whenever we place data in a set, must evict whatever is there
- Associativity $>1 \rightarrow$ **set-associative caches**
 - Can keep multiple cache blocks that would map to the same set
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2-way set-associative cache (associativity = 2)



2-way set-associative cache (associativity = 2)

A = 2: Two blocks per set

Assume: block size 8 bytes

Address of short:

compare both

valid? + tag match? if yes → hit

v tag 7 6 5 4 3 2 1 0 v tag 7 6 5 4 3 2 1 0

block offset

The data we want is either on the left, or on the right, or not in the cache at all. It can't be anywhere else! Addresses map to a single set!

2-way set-associative cache (associativity = 2)

A = 2: Two blocks per set Assume: block size 8 bytes Address of short: 0...01 t bits 100 compare both valid? + tag match? if yes = hit 7 6 5 4 7 6 5 4 3 block offset

If no match:

• One block in set is selected for eviction and replacement

short is here (2 bytes)

- Replacement policies: random, least recently used (LRU), ...
 - More clever → lower miss rate, but harder to implement in hardware

2-way set-associative cache simulation

M=16 addresses, byte-addressable, B=2 bytes/block, K=2 sets, A=2 blocks/set Same total size and block size as before. Associativity (and thus # of sets) changed.

t=2	s=1	b=1
XX	Х	X

Address trace (reads, one byte per read):

0	[00]	0	0_{2}]	miss
1	[00]	0	1_{2}^{-}	hit
7	[01	1	1_{2}^{-}	miss
8	[10	0	0_{2}^{-}	miss
0	[00]	0	0_{2}^{-}	hit

The same address sequence in the direct mapped cache resulted in:
miss
hit Higher associativity =
Less likely to have to evict!
miss
miss
Temporal locality: want data in cache to stay in cache!

	V	Tag	Block
Set 0	1	00	M[1-0]
	1	10	M[9-8]

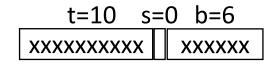
Pause for questions on set-associative caches

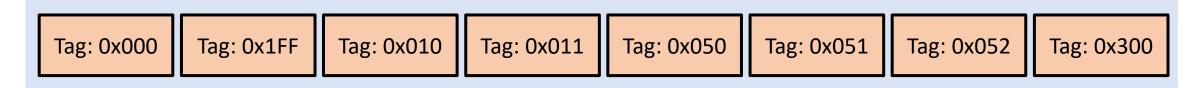
Fully-associative caches

- What changes with fully-associative caches?
 - Anything can go anywhere
 - Only one set (s = 0 bits)

- Otherwise, same steps as for a set-associative cache
 - Compare tag against all blocks in the set

- Fully-associative cache on a 16-bit system
 - One set (fully associative!)
 - Eight, 64-byte blocks



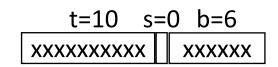


- Are the following addresses in the cache?
 - 0x0400
 - 0x0410
 - 0xC002
 - 0xC048

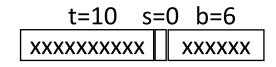
- Fully-associative cache on a 16-bit system
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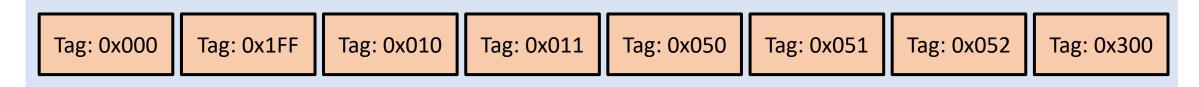
t=??	s=	0 b=??
. 55		??

- Fully-associative cache on a 16-bit system
 - One set (fully associative!)
 - Eight, 64-byte blocks



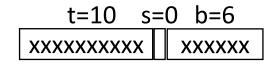
- Fully-associative cache on a 16-bit system
 - One set (fully associative!)
 - Eight, 64-byte blocks

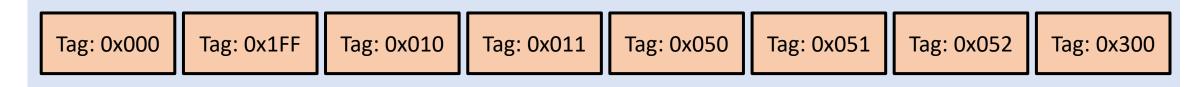




- Are the following addresses in the cache?
 - 0x0400⇒0b0000 0100 0000 0000
 - 0x0410⇒0b0000 0100 0001 0000
 - 0xC002⇒0b1100 0000 0000 0010
 - 0xC048⇒0b1100 0000 0100 1000

- Fully-associative cache on a 16-bit system
 - One set (fully associative!)
 - Eight, 64-byte blocks



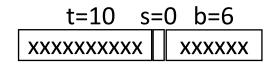


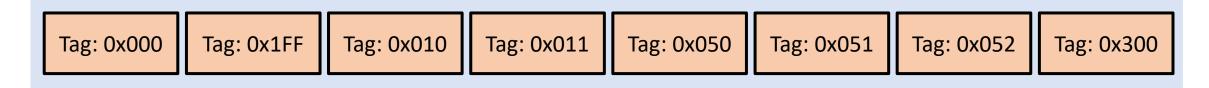
- Are the following addresses in the cache?
 - $0x0400 \Rightarrow 0b0000 0100 0000 0000 → Tag 0x010$
 - $0x0410 \Rightarrow 0b0000 0100 0000 01 0000 \rightarrow Tag 0x010 (same block!)$
 - 0xC002⇒0b<u>1100 0000 00</u>00 0010
 - 0xC048⇒0b<u>1100 0000 01</u>00 1000

HIT

HIT

- Fully-associative cache on a 16-bit system
 - One set (fully associative!)
 - Eight, 64-byte blocks





- Are the following addresses in the cache?
 - 0x0400 ⇒ 0b0000 0100 00000 00000 → Tag 0x010 HIT

 - $0xC002 \Rightarrow 0b1100 0000 0000 0010 \rightarrow Tag 0x300$
 - $0xC048 \Rightarrow 0b\underline{1100\ 0000\ 01}00\ 1000 \rightarrow Tag\ 0x301$ (different block!) **MISS**

HIT

Associativity Pros and Cons

Direct-mapped

- Simplest to implement: look-up compares tag with 1 cache block
 → requires fewer transistors, which can be used elsewhere on the chip
- Conflicts can easily lead to thrashing
 - Two cache blocks map to the same set, program needs both, and they keep kicking each other out of the cache. Lots of misses. Bad times.

Set-associative

- More complex implementation: requires more (HW) tag comparators
- Lower miss rate than direct-mapped caches (fewer conflict misses)
 - 2-way is a significant improvement over direct-mapped
 - 4-way is a more modest improvement over 2-way, and so on

Fully-associative

- One comparator per cache block in the cache means a LOT of hardware. Ouch.
 - Often a deal-breaker for hardware
- Very low miss rate!

Intel Core i7 Cache Hierarchy

Processor package Core 0 Core 3 Regs Regs L1 L1 L1 d-cache i-cache d-cache i-cache L2 unified L2 unified cache cache L3 unified cache (shared by all cores)

Main memory

L1 i-cache and d-cache:

32 KB, 8-way,

Access: 4 cycles

Keep separate caches for instructions and data. Don't want them to step on each other's toes!

L2 unified cache:

256 KB, 8-way,

Access: 11 cycles

L3 unified cache:

8 MB, 16-way,

Access: 30-40 cycles

Last resort before going to main memory (slow!) So want this large and highly-associative, to have very few misses.

Block size: 64 bytes for all caches.

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Cache Performance Metrics

Miss Rate

- Fraction of memory references not found in cache (misses / accesses) = 1 hit rate
- Typical numbers (in percentages):
 - 3-10% for L1
 - Can be quite small (e.g., < 1%) for L2, depending on dataset size, etc.
 - However, many applications have >30% miss rate in L2 cache

Hit Time

- Time to deliver a block in the cache to the processor
 - Includes time to determine whether the block is in the cache
- Typical numbers:
 - 1-2 clock cycles for L1
 - 5-20 clock cycles for L2

Miss Penalty

- Additional time required because of a miss
- Typically 50-200 cycles for main memory
 - Not really a "penalty", just how long it takes to read from memory

Let's think about those numbers

- Huge difference between a hit and a miss
 - Could be 100x, if comparing L1 and main memory
- Would you believe a 99% hit rate is twice as good as 97%?
 - Consider: cache hit time of 1 cycle miss penalty of 100 cycles
 - Average access time:

```
97% hits: 100 instructions: 100 cycles (1 per instruction) + 3*100 (misses) on average: 1 cycle/instr. + 0.03 * 100 cycles/instr. = 4 cycles/instr. 99% hits: on average: 1 cycle/instr. + 0.01 * 100 cycles/instr. = 2 cycles/instr.
```

- This is why "miss rate" is used instead of "hit rate"
 - In our example, 1% miss rate vs. 3% miss rate
 - Makes the radical performance difference more obvious
- "Computation is what happens between cache misses."

Average Memory Access Time (AMAT)

- AMAT = Hit time + Miss rate \times Miss penalty
 - Generalization of previous formula
- Can extend for multiple layers of caching
 - AMAT = Hit Time L1 + Miss Rate L1 × Miss Penalty L1
 - Miss Penalty L1 = Hit Time L2 + Miss Rate L2 × Miss Penalty L2
 - Miss Penalty L2 = Hit Time Main Memory

Multi-level caching helps minimize AMAT

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