

Run-Time Polymorphism

CS 211

Definition

polymorphism, n. (from poly- + -morphism)

1. The ability to assume different forms or shapes.
2. (biology) The coexistence, in the same locality, of two or more distinct forms independent of sex, not connected by intermediate gradations, ...
3. (object-oriented programming) The feature pertaining to the dynamic treatment of data elements based on their type, allowing for an instance of a method to have several definitions.
4. (mathematics, type theory) The property of certain typed formal systems of allowing for the use of type variables and binders/quantifiers over those type variables; ...
5. (crystallography) ...
6. (genetics) ...

Parametric polymorphism (in OCaml)

```
let reverse xs0 =  
  let rec loop acc xs =  
    match xs with  
    | []          -> acc  
    | x :: xs'   -> loop (x :: acc) xs'  
  in loop [] xs0
```

ML stands for meta-language

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OCaml infers a polymorphic type:

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reverse : 'a list -> 'a list
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reverse : 'a list -> 'a list
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In C++ syntax:

```
template<class T>  
List<T> reverse(List<T>);
```

Ad-hoc polymorphism

Also known as overloading:

```
bool test(int v, int lo, int hi)
{
    return lo <= v && v < hi;
}
```

```
bool test(double v, double lo, double hi)
{
    return low <= v && v <= hi;
}
```

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Overloading is dispatched statically.

Generic = parametric + ad-hoc

```
template<class T>
void filter(std::vector<T>& v, T lo, T hi)
{
    size_t dst = 0;

    for (T x : v) {
        if (test(x, lo, hi)) {
            v[dst++] = x;
        }
    }

    v.resize(dst);
}
```

Message/method polymorphism

```
Number subclass: Complex [  
  | realpart imagpart |  
  
  "constructor and setter omitted..."  
  
  real [ ^realpart ]  
  imag [ ^imagpart ]  
  
  + other [  
    ^Complex real: (realpart + other real)  
              imag: (imagpart + other imag)  
  ]  
  
  "etc..."  
]
```

Subtype polymorphism in theory

A type τ is a subtype of a type σ (notation: τ **is-a** σ) **iff** every value of type τ is also a value of type σ .

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Possible examples:

- `int is-a double?`

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- Rectangle **is-a** Shape ?

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Possible examples:

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- Rectangle **is-a** Shape
- Square **is-a** Rectangle ?

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- Rectangle **is-a** Shape
- Square **is-a** Rectangle
- `vector<Rectangle>` **is-a** `vector<Shape>` ?

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Possible examples:

- Integer **is-a** Real
- Rectangle **is-a** Shape
- Square **is-a** Rectangle
- `vector<Rectangle>` **is-a** `vector<Shape>`
- `bool (*) (Shape)` **is-a** `bool (*) (Rectangle)` ?

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Possible examples:

- Integer **is-a** Real
- Rectangle **is-a** Shape
- Square **is-a** Rectangle
- `vector<Rectangle>` **is-a** `vector<Shape>`
- `bool (*) (Rectangle)` **is-a** `bool (*) (Shape)`

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Possible examples (but in C++, **indirection** is required):

- `Integer& is-a Real&`
- `Rectangle& is-a Shape&`
- `Square is-a Rectangle`
- `vector<Rectangle> is-a vector<Shape>`
- `bool (*)(Rectangle&) is-a bool (*)(Shape&)`

Subtype polymorphism in C++

```
struct Base  
{ int x; };
```

```
struct Derived : Base  
{ int y; };
```

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```
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```
struct Derived : Base  
{ int y; };
```

Then:

- Derived* **is-a** Base*,
- Derived& **is-a** Base&, and
- and likewise for `const` versions, but
- ~~Derived **is-a** Base~~ – why not?

Adding “methods”

```
struct Base  
{ int f() { return 0; } };
```

```
struct Derived : Base  
{ int f() { return 1; } };
```

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struct Base
{ int f() { return 0; } };
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struct Derived : Base
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```

```
TEST_CASE("direct")
{
    Base b;
    Derived d;
    CHECK( b.f() == 0 );
    CHECK( d.f() == 1 );
}
```

Adding “methods”

```
struct Base
{ int f() { return 0; } };
```

```
struct Derived : Base
{ int f() { return 1; } };
```

```
int g(Base& b) { return b.f(); }
```

```
TEST_CASE("via reference")
{
    Base b;
    Derived d;
    CHECK( g(b) == 0 );
    CHECK( g(d) == 0 ); // ???
}
```

Static versus dynamic dispatch

To determine which function to call:

- Static dispatch uses the static type of the variable
- Dynamic dispatch uses the run-time class of the object

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To get dynamic dispatch in C++, a function must be **virtual**

Introducing virtual functions

```
struct Base
{ virtual int f() { return 0; } };

struct Derived : Base
{ int f() override { return 1; } };
```

Introducing virtual functions

```
struct Base
{ virtual int f() { return 0; } };
```

```
struct Derived : Base
{ int f() override { return 1; } };
```

```
int g(Base& b) { return b.f(); }
```

```
TEST_CASE("via reference")
{
    Base b;
    Derived d;
    CHECK( g(b) == 0 );
    CHECK( g(d) == 1 );
}
```

